

DECISION PROCEDURE FOR TRACE EQUIVALENCE

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CONTEXT

■ Cryptographic protocols

Most communications take place over a **public** network



Cryptographic protocols

- small programs designed to secure communication (e.g. secrecy)
- use cryptographic primitives (e.g. encryption, signature)

It important to ensure their security

CONTEXT

- Reliable cryptography
- **Correct specification**
- Implementation satisfying the specification

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- Some security properties

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Reachability properties

- Secrecy, Authentication, ...

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Reachability properties

- Secrecy, Authentication, ...

Equivalence properties

- Anonymity, Privacy, Receipt-Freeness, ...

CONTEXT

- Modeling security properties



Alice



Bob

CONTEXT

- Modeling security properties



Alice



Bob

CONTEXT

- Modeling security properties



Alice



Intruder



Bob

The intruder can

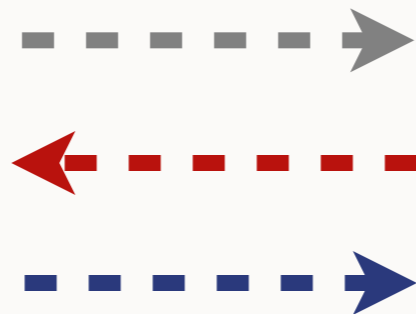
- intercept all messages
- transmit or modify messages
- test equality between messages
- initiate several sessions

CONTEXT

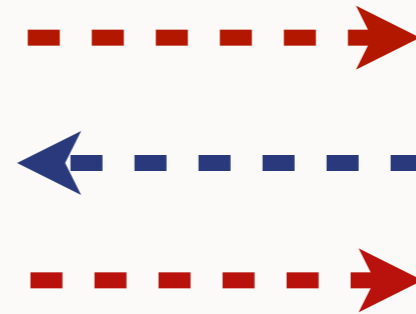
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The intruder can

- intercept all messages
- transmit or modify messages
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- initiate several sessions

CONTEXT

- Reachability properties : secrecy, authentication,...



Alice



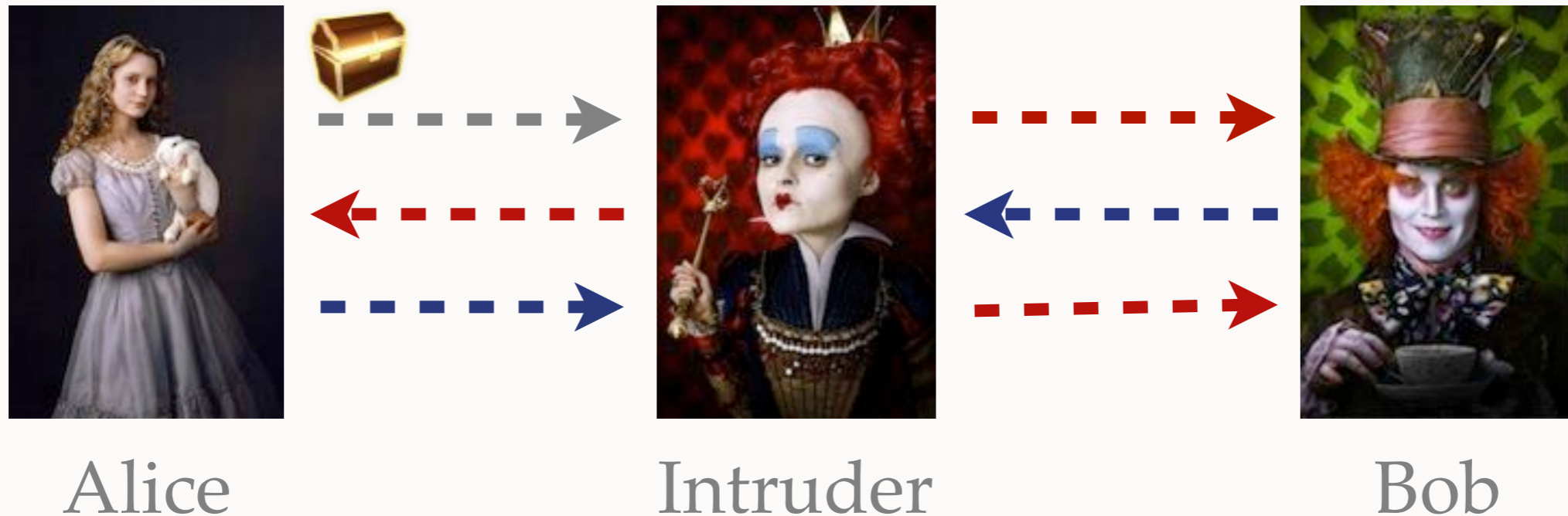
Intruder



Bob

CONTEXT

- Reachability properties : secrecy, authentication,...

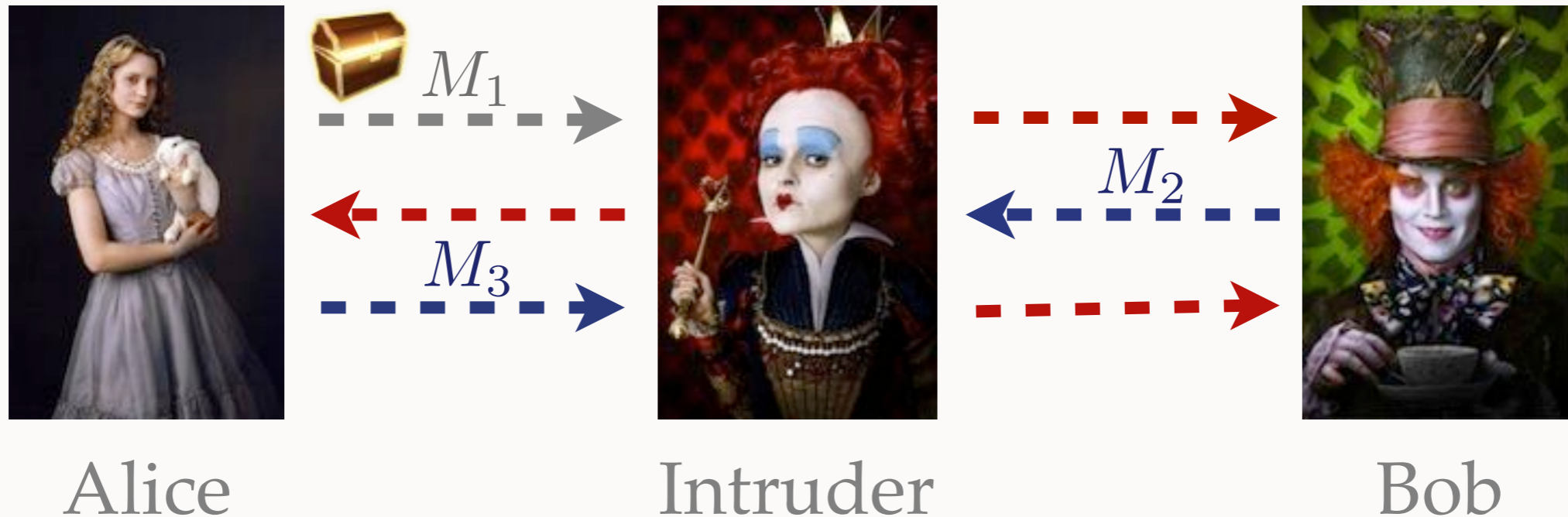


Can the intruder deduce Alice's secret ?

CONTEXT

- Reachability properties : secrecy, authentication,...

intruder's knowledge : $M_1 M_2 M_3$ + basic knowledge



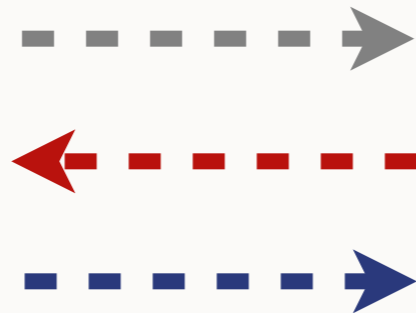
Can the intruder deduce Alice's secret ?

CONTEXT

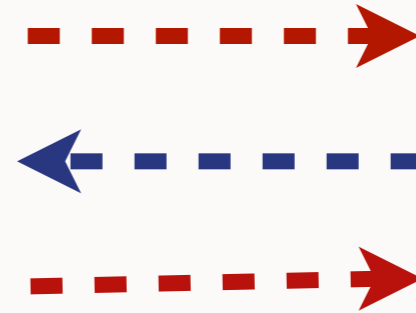
- Equivalence properties : strong secret, anonymity,...



Alice



Intruder



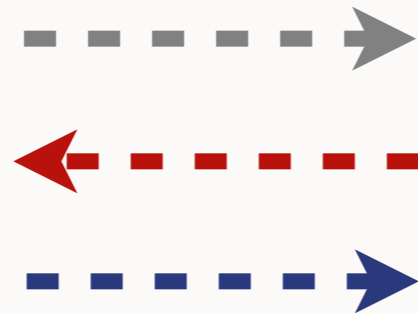
Unknown

CONTEXT

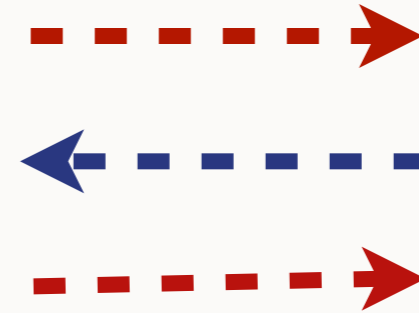
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Alice



Intruder



Unknown

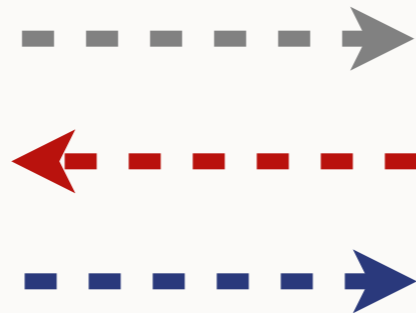
Can the intruder deduce the unknown's identity ?

CONTEXT

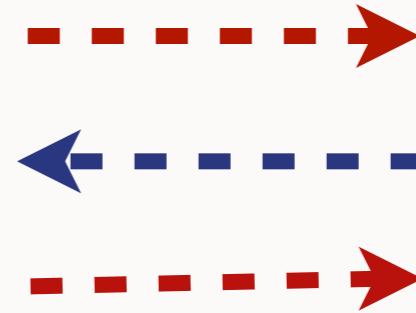
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Alice



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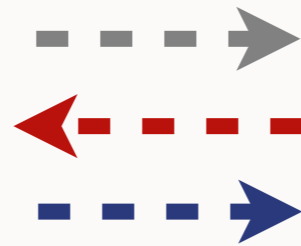
Unknown

CONTEXT

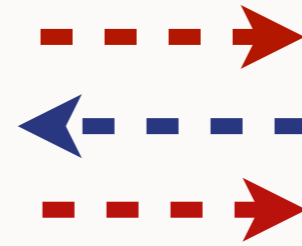
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Alice



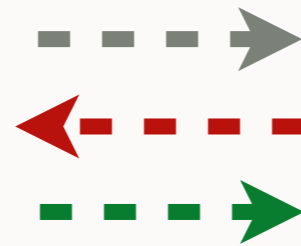
Intruder



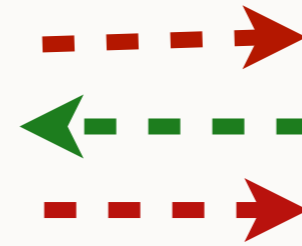
Unknown



Alice



Intruder



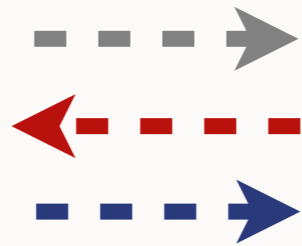
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CONTEXT

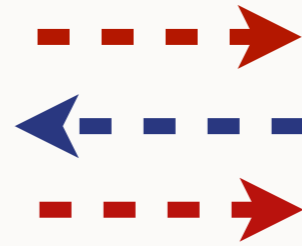
- Equivalence properties : strong secret, anonymity,...



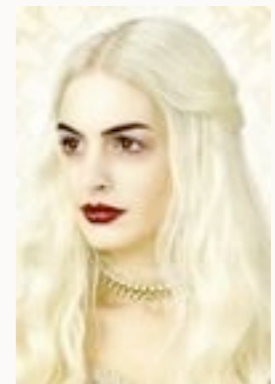
Alice



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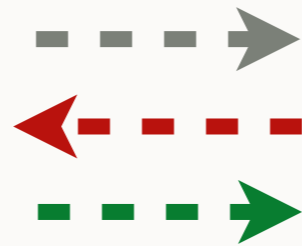
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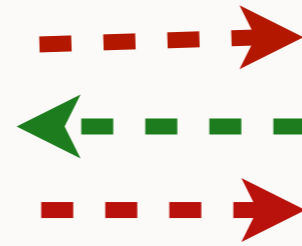
Charlene



Alice



Intruder



Unknown



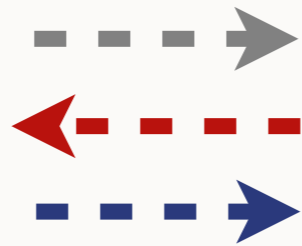
Bob

CONTEXT

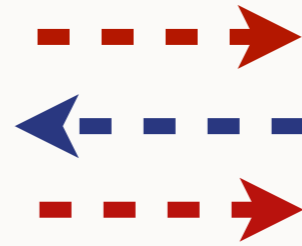
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Alice



Intruder



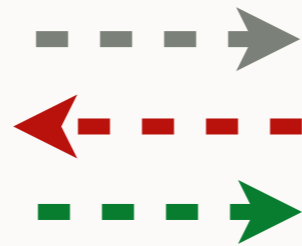
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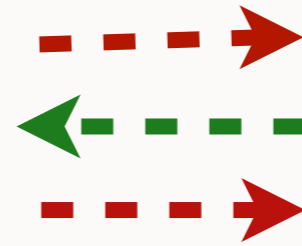
Charlene



Alice



Intruder



Unknown



Bob

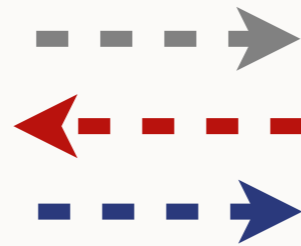
Can the intruder distinguish the two situations ?

CONTEXT

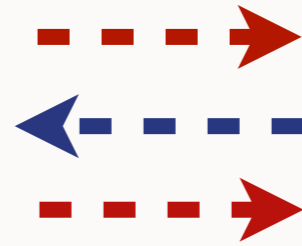
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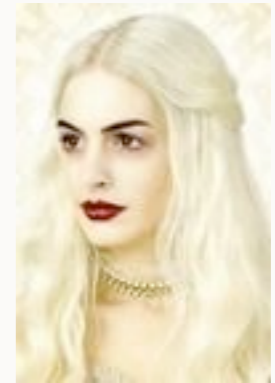
Alice



Intruder



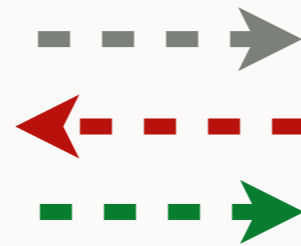
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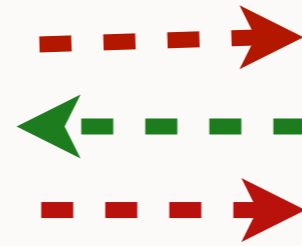
Charlene



Alice



Intruder



Unknown



Bob

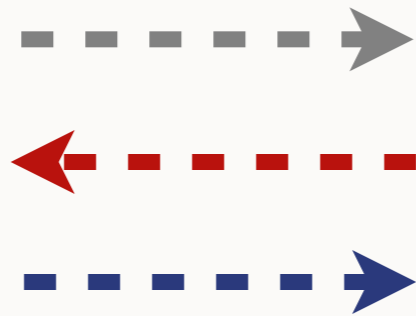
Trace Equivalence

PREVIOUS WORKS

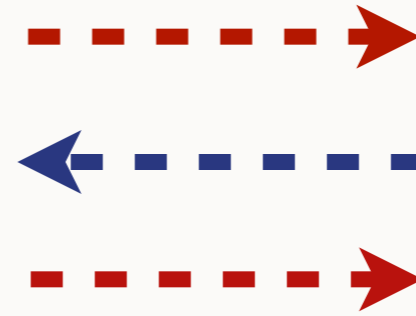
- Knowledge indistinguishability : static equivalence



Alice



Intruder



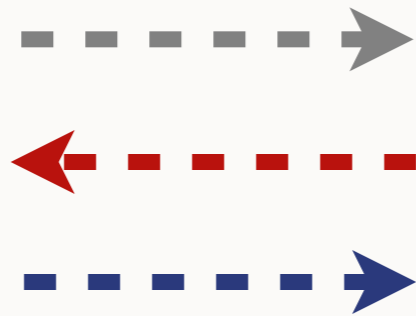
Bob

PREVIOUS WORKS

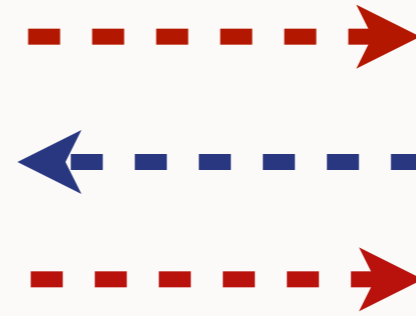
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Intruder



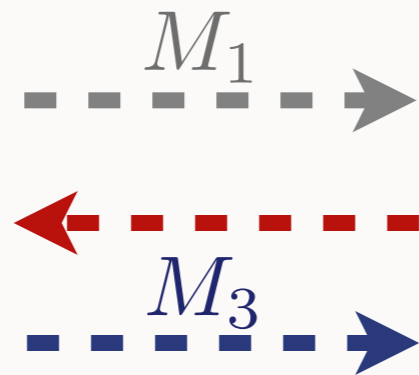
Bob

PREVIOUS WORKS

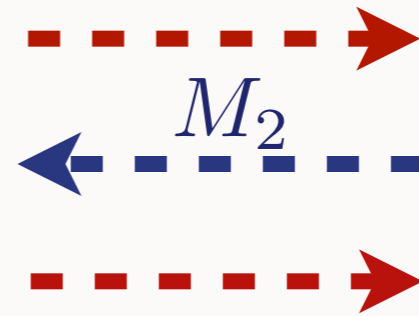
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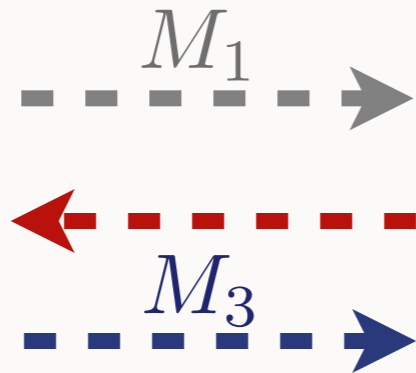
Bob

PREVIOUS WORKS

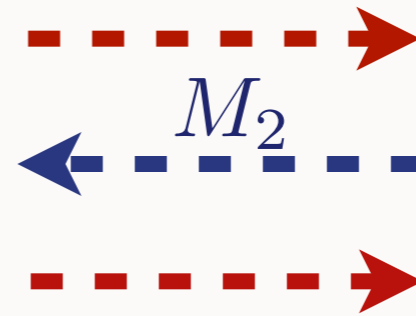
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Alice



Intruder



Bob

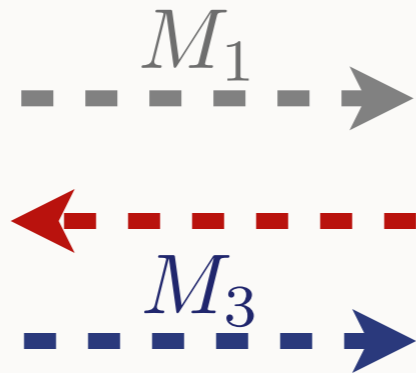
Example with decryption : $dec(\{x\}_y, y) = x$

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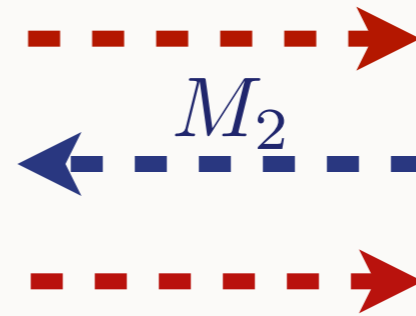
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Intruder



Bob

Example with decryption : $dec(\{x\}_y, y) = x$

$$\Phi_1 : a, \{b\}_a, b$$

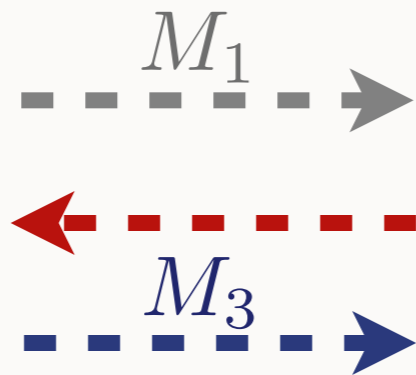
$$\Phi_2 : c, \{b\}_a, b$$

PREVIOUS WORKS

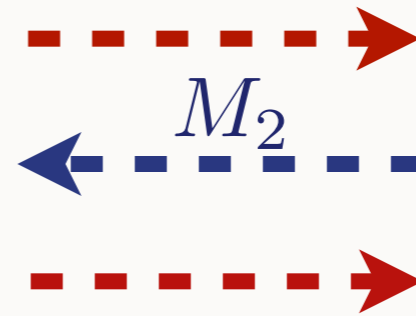
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Alice



Intruder



Bob

Example with decryption : $dec(\{x\}_y, y) = x$

$$dec(M_2, M_1) = M_3$$

$$\Phi_1 : a, \{b\}_a, b$$

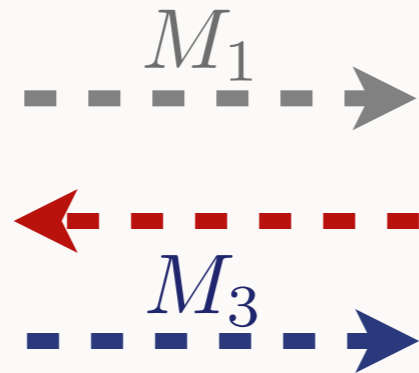
$$\Phi_2 : c, \{b\}_a, b$$

PREVIOUS WORKS

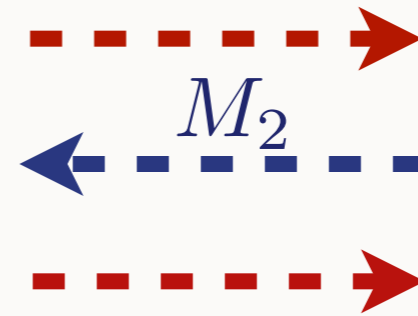
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Alice



Intruder



Bob

Example with decryption : $dec(\{x\}_y, y) = x$

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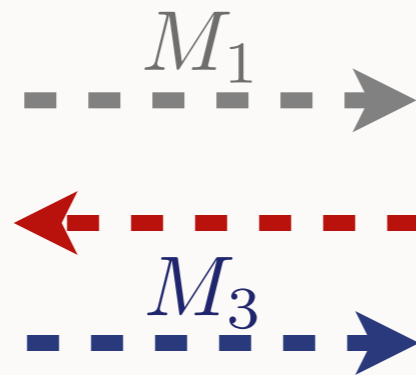
$$dec(\{b\}_a, c) \neq b$$

PREVIOUS WORKS

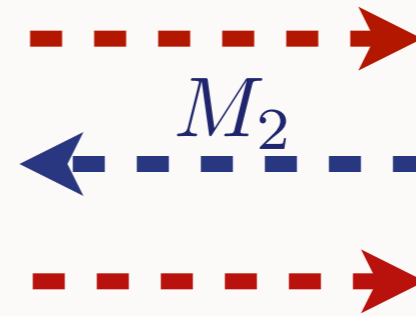
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Alice



Intruder



Bob

Example with decryption : $dec(\{x\}_y, y) = x$

$$dec(M_2, M_1) = M_3$$

$$\Phi_1 : a, \{b\}_a, b \quad dec(\{b\}_a, a) = b$$

$$\Phi_2 : c, \{b\}_a, b \quad dec(\{b\}_a, c) \neq b$$

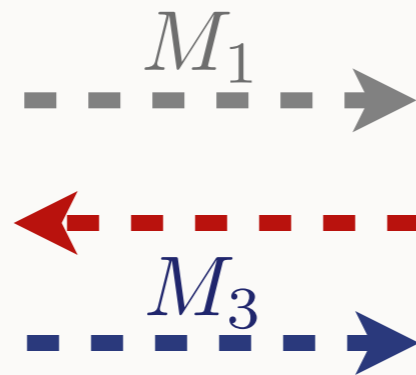
Not equivalent

PREVIOUS WORKS

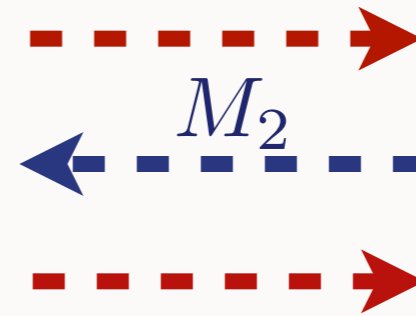
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Alice



Intruder



Bob

Example with decryption : $dec(\{x\}_y, y) = x$

$\Phi_1 : a, \{b\}_a, b$	$dec(\{b\}_a, a) = b$	$\Phi_1 : a, \{b\}_a$ $\Phi_2 : c, \{b\}_a$
$\Phi_2 : c, \{b\}_a, b$	$dec(\{b\}_a, c) \neq b$	

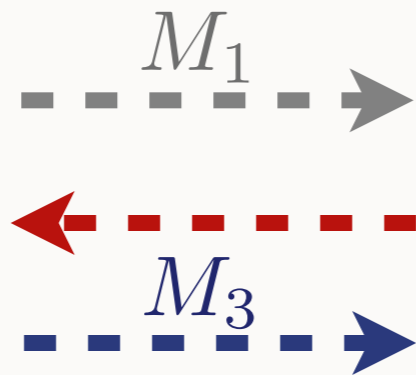
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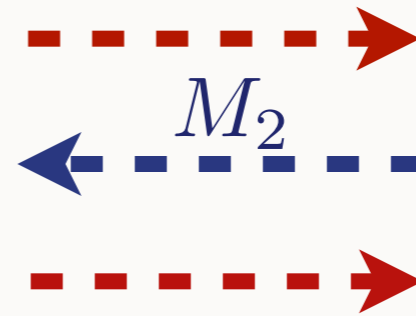
- Knowledge indistinguishability : static equivalence



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Intruder



Bob

Example with decryption : $dec(\{x\}_y, y) = x$

	$dec(M_2, M_1) = M_3$	
$\Phi_1 : a, \{b\}_a, b$	$dec(\{b\}_a, a) = b$	
$\Phi_2 : c, \{b\}_a, b$	$dec(\{b\}_a, c) \neq b$	

$\Phi_1 : a, \{b\}_a$
$\Phi_2 : c, \{b\}_a$

No test

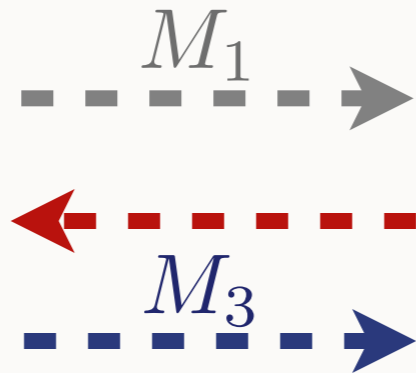
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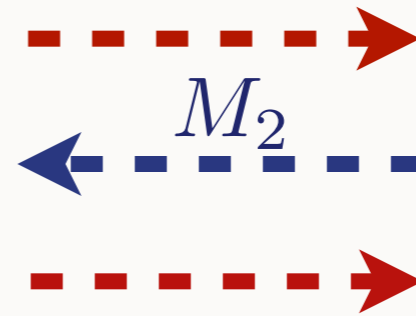
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Example with decryption : $dec(\{x\}_y, y) = x$

$\Phi_1 : a, \{b\}_a, b$ $dec(M_2, M_1) = M_3$
 $dec(\{b\}_a, a) = b$
 $\Phi_2 : c, \{b\}_a, b$ $dec(\{b\}_a, c) \neq b$

Not equivalent

$\Phi_1 : a, \{b\}_a$
 $\Phi_2 : c, \{b\}_a$

No test

Equivalent

PREVIOUS WORKS

Most of the previous works focus on stronger equivalence

- A. Tiu and J. E. Dawson. *Automating open bisimulation checking for the spi calculus.*
- M. Baudet. *Sécurité des protocoles cryptographiques : aspects logiques et calculatoires.* Phd thesis
- B. Blanchet, M. Abadi, and C. Fournet. *Automated verification of selected equivalences for security protocols.*
 - ➔ Tool : B. Blanchet, *ProVerif*

Trace equivalence for simple processes without else branches

- V. Cortier and S. Delaune. *A method for proving observational equivalence.*

MOTIVATION

■ Example

Two problematic examples :

- e-passport protocols : M. Arapinis, T. Chothia, E. Ritter, and M. Ryan. *Analysing unlinkability and anonymity using the applied pi calculus.*
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MOTIVATION

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Alice

$\{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}$

----->



Bob

MOTIVATION

■ Example

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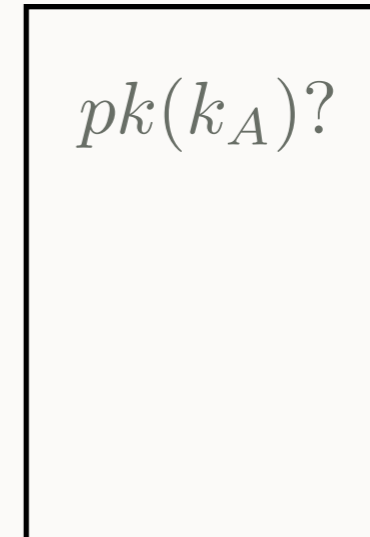
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Bob

MOTIVATION

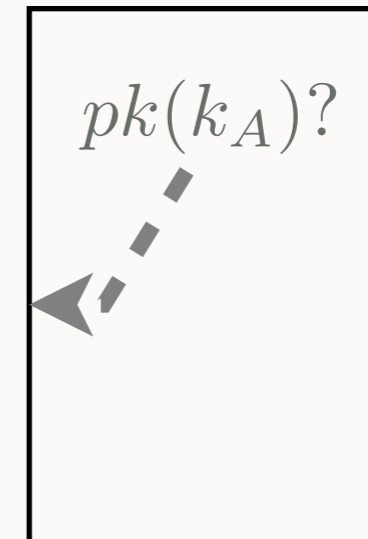
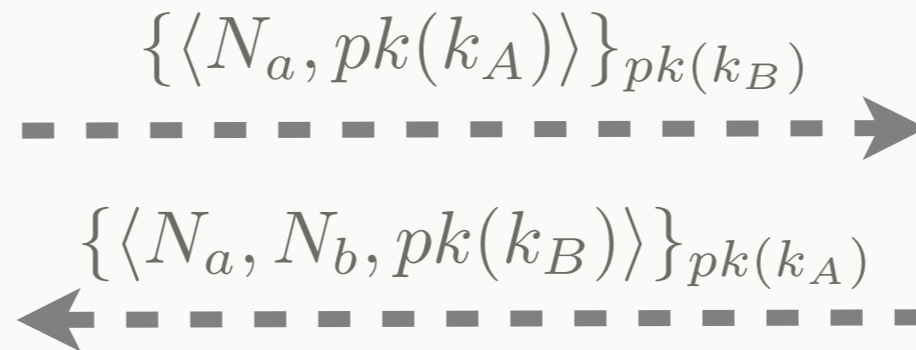
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MOTIVATION

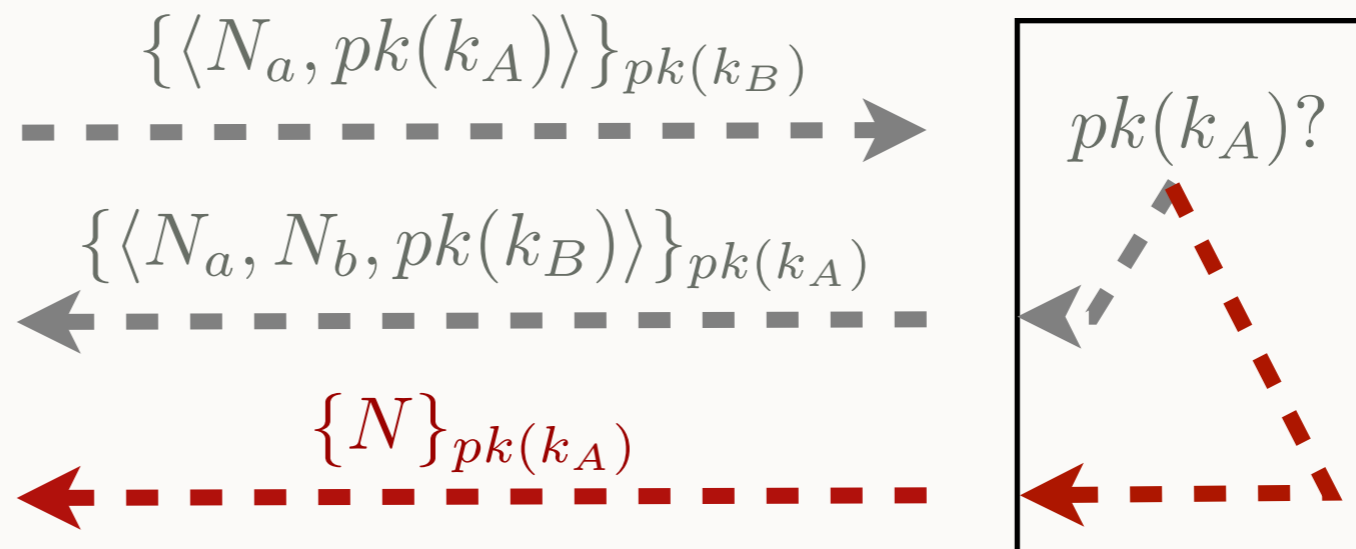
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MOTIVATION

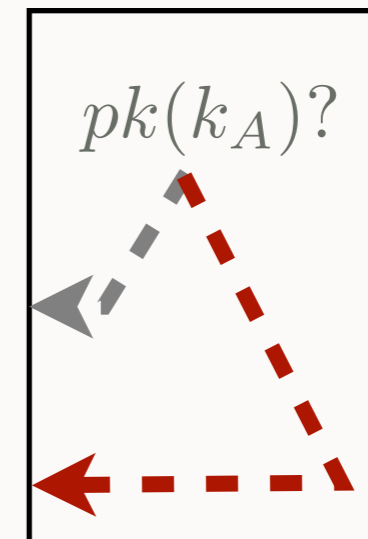
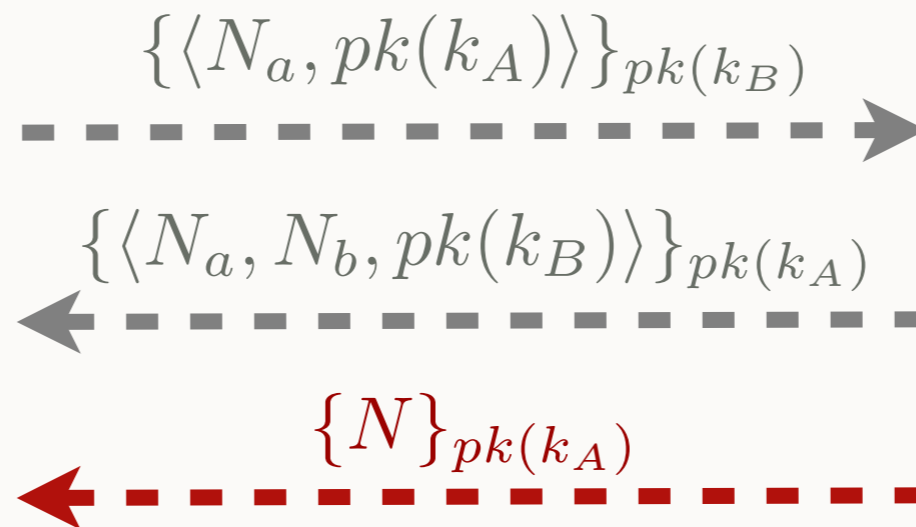
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Unknown



Bob

MOTIVATION

- Example



Alice



Intruder



Bob



Charlene



Intruder



Bob

MOTIVATION

- Example



Alice



Bob



Charlene



Bob

MOTIVATION

- Example



Alice

$\{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}$
----->



Bob



Charlene



Bob

MOTIVATION

- Example



Alice

$\{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}$ →

$\{\langle x, y \rangle\}_{pk(k_B)}$ →



Bob



Charlene



Bob

MOTIVATION

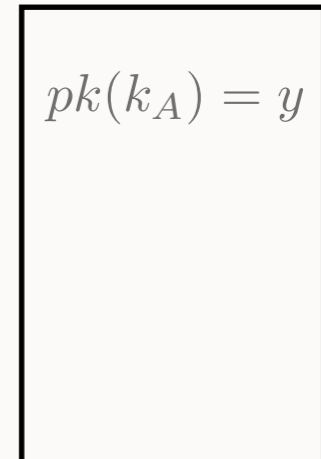
- Example



Alice

$\{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}$ →

$\{\langle x, y \rangle\}_{pk(k_B)}$ →



Bob



Charlene



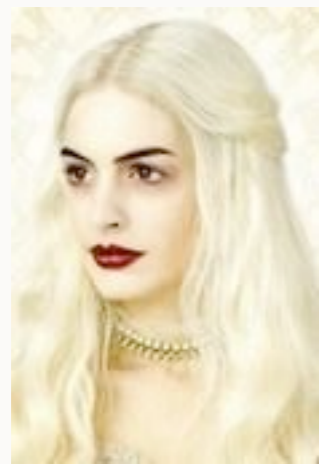
Bob

MOTIVATION

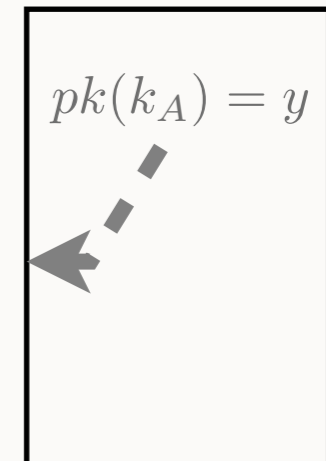
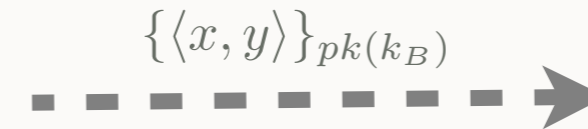
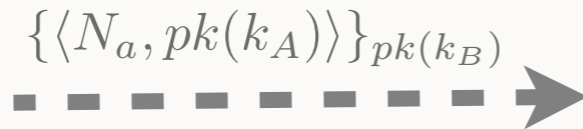
■ Example



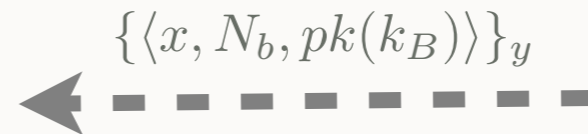
Alice



Charlene



Bob



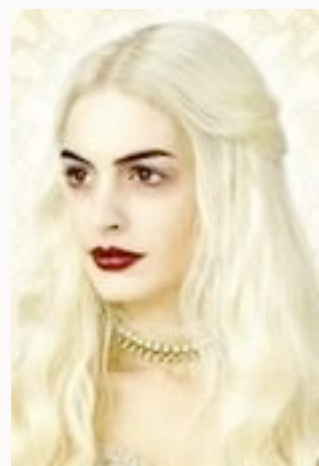
Bob

MOTIVATION

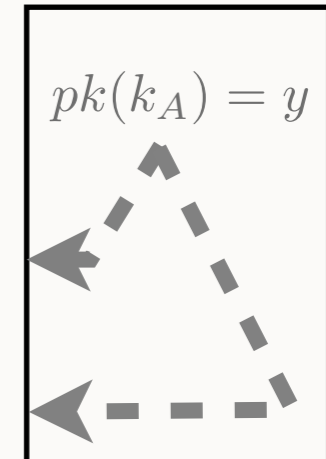
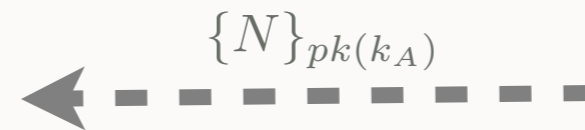
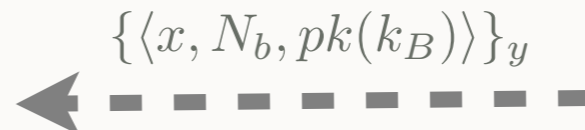
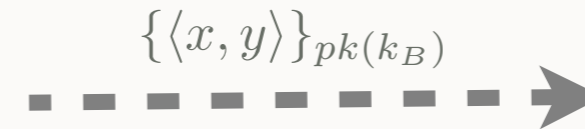
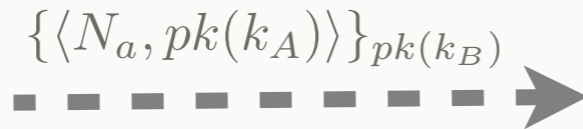
■ Example



Alice



Charlene



Bob



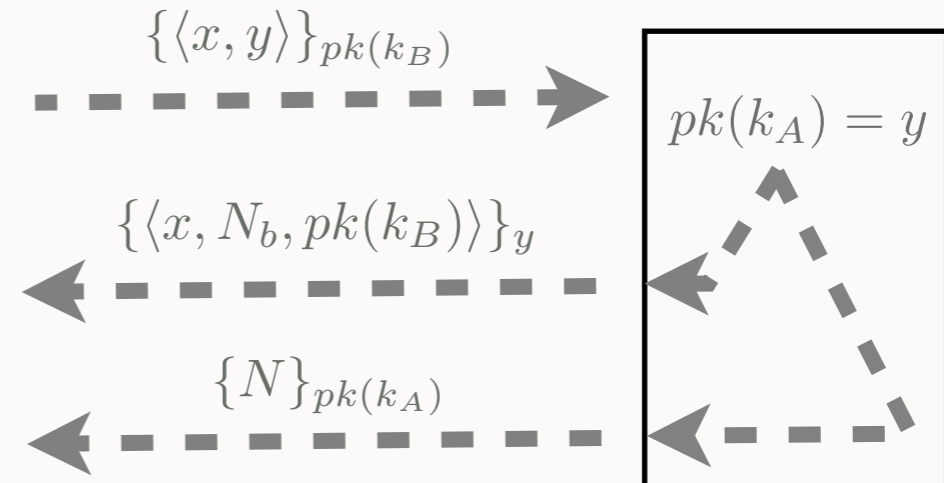
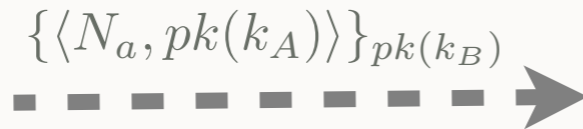
Bob

MOTIVATION

■ Example



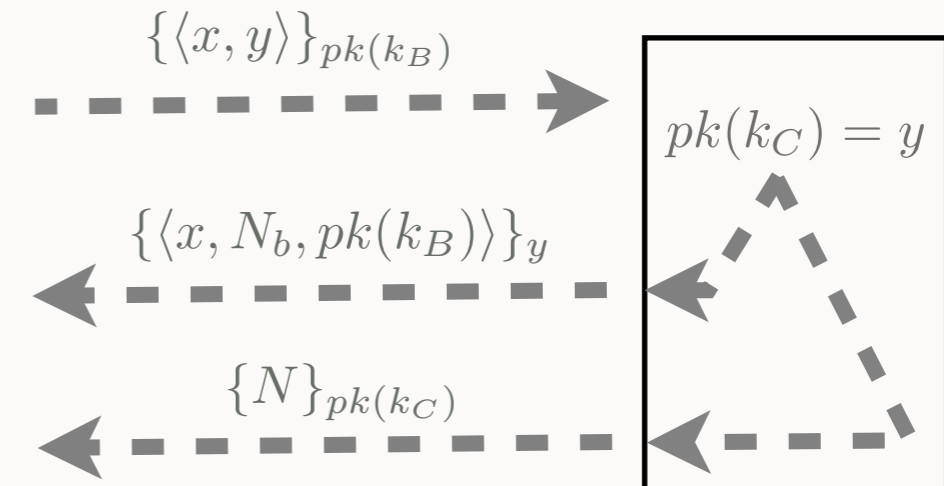
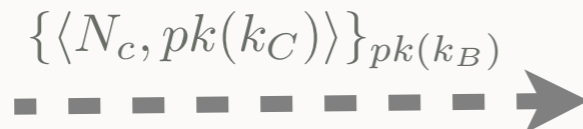
Alice



Bob



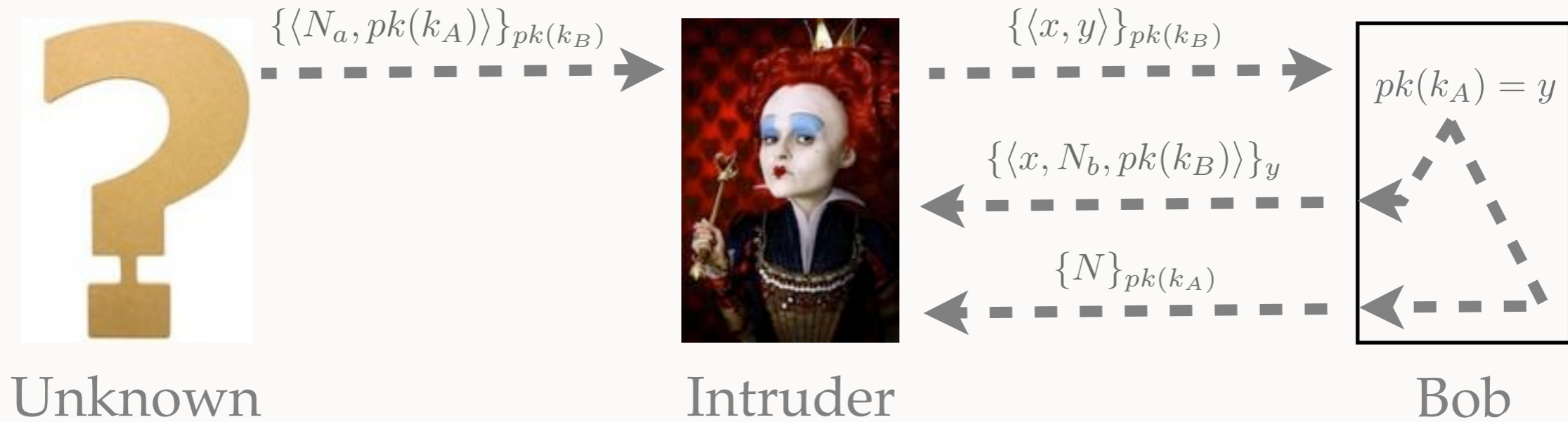
Charlene



Bob

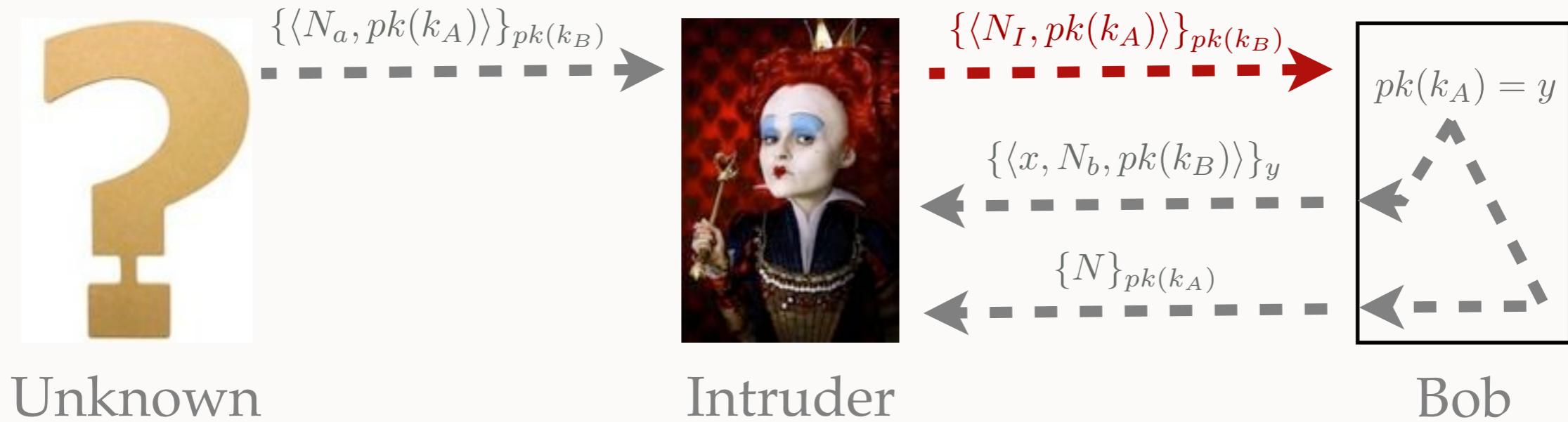
MOTIVATION

■ Example



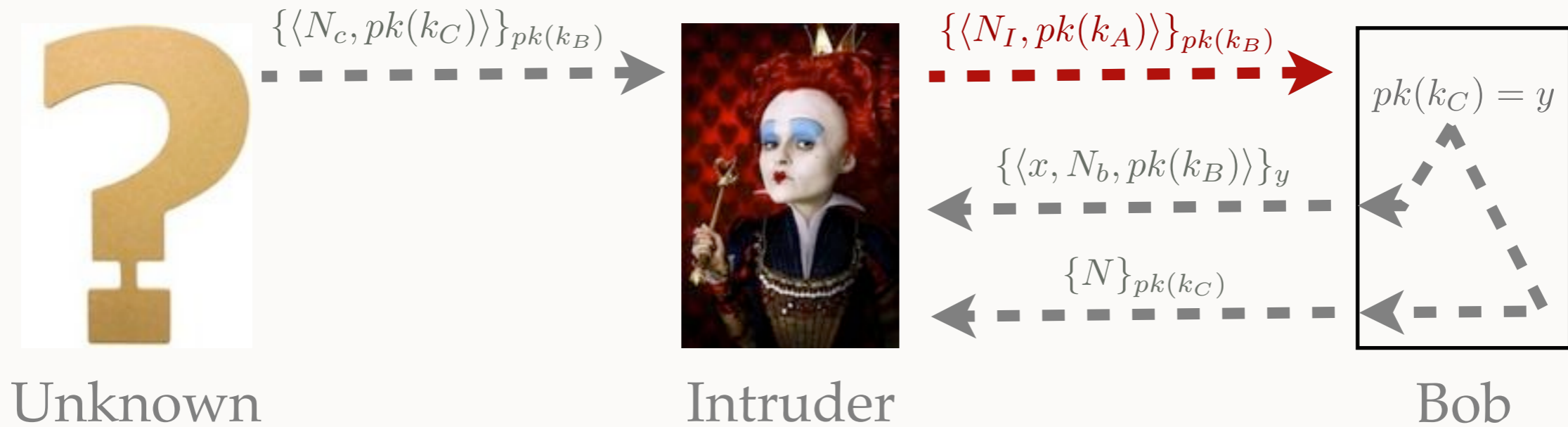
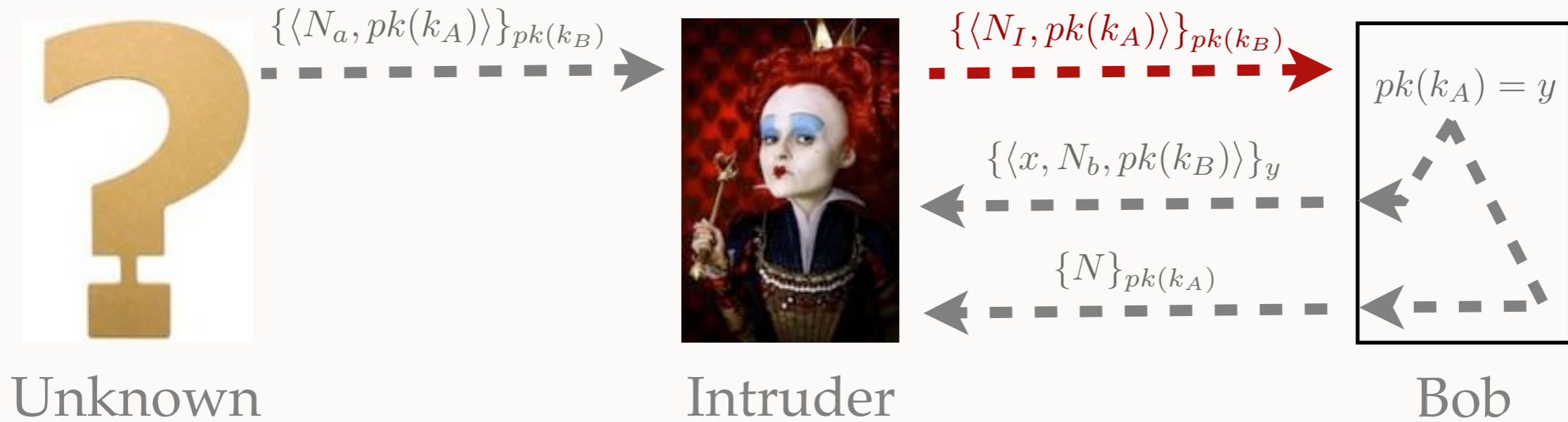
MOTIVATION

■ Example



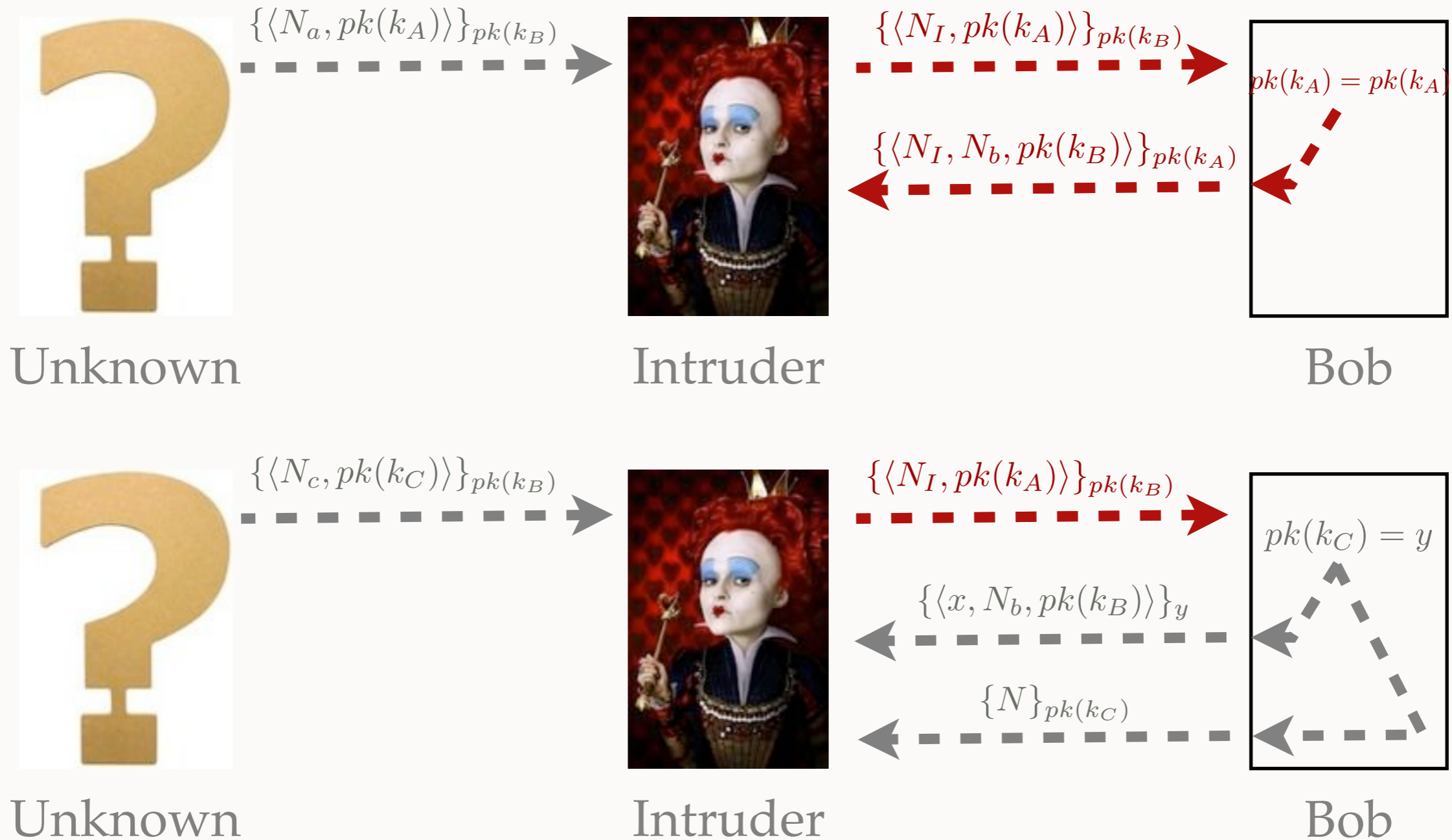
MOTIVATION

■ Example



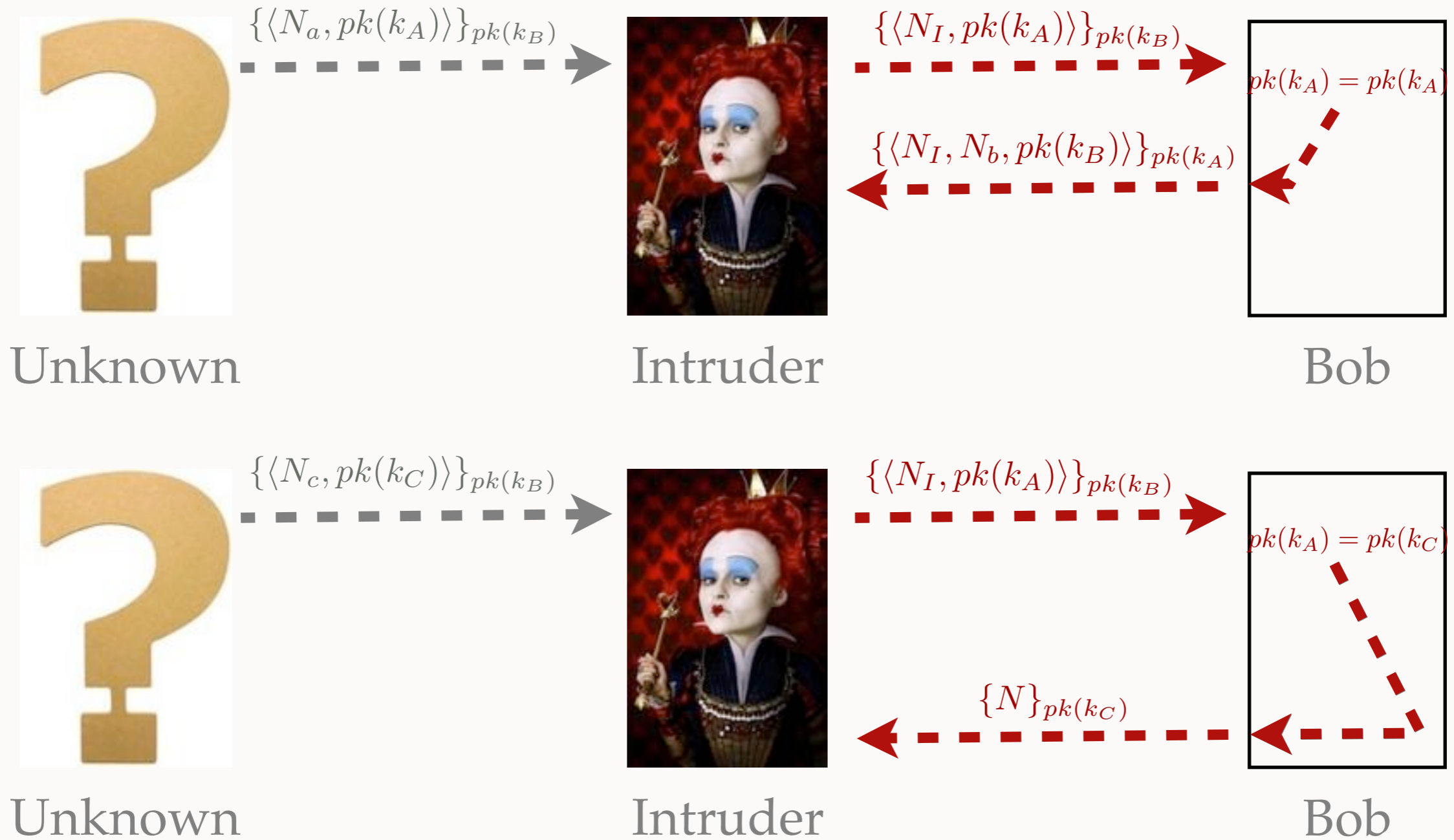
MOTIVATION

■ Example



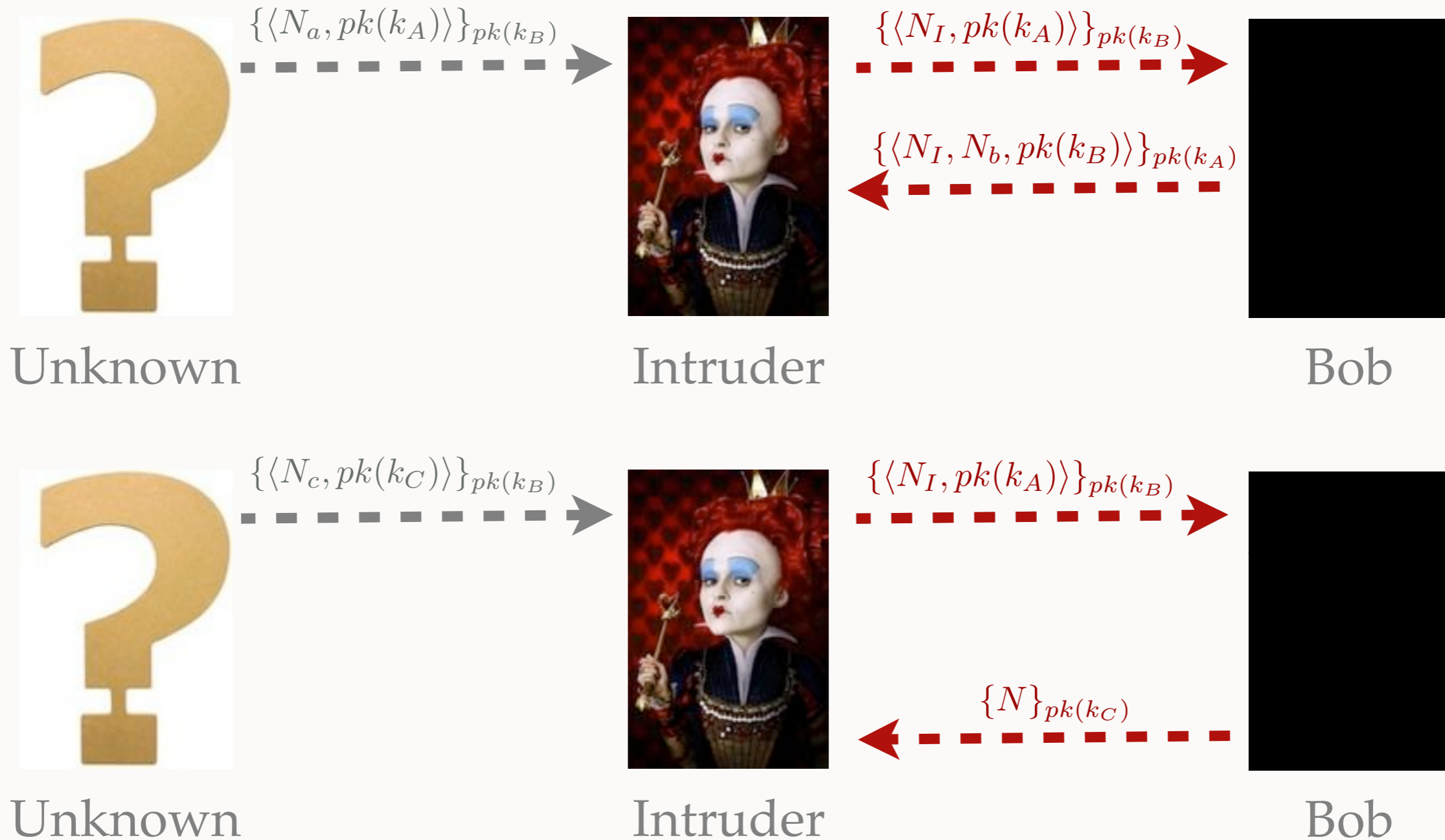
MOTIVATION

■ Example



MOTIVATION

■ Example



CONTRIBUTION

Decision procedure for trace equivalence

- Infinitely many traces are represented by symbolic constraint system
- + Protocol possibly non-determinist and with non trivial else branches
- + Private channels
- Finite set of cryptographic primitives : symmetric and asymmetric encryption, pairing and signature
- Bounded number of sessions (no replication in the process algebra)

CONSTRAINT SYSTEM

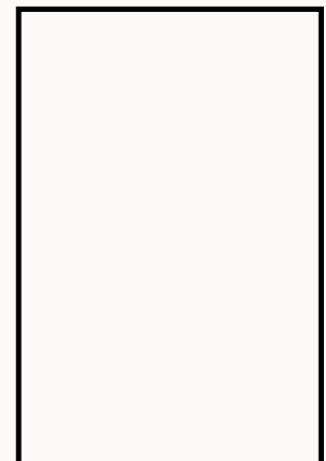
- One constraint system = one interleaving = several traces



Alice



Intruder



Bob

CONSTRAINT SYSTEM

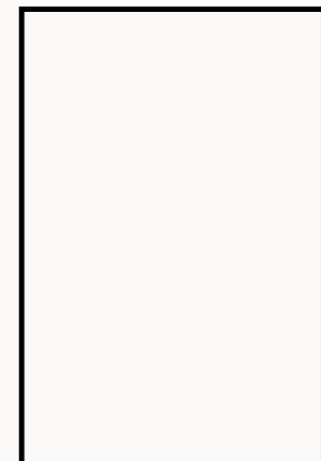
- One constraint system = one interleaving = several traces



Alice



Intruder



Bob

$pk(k_A), pk(k_B), pk(k_C), N_I$

CONSTRAINT SYSTEM

- One constraint system = one interleaving = several traces



Alice

$\{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}$
----->



Intruder



Bob

$pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}$

CONSTRAINT SYSTEM

- One constraint system = one interleaving = several traces



$$pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)} \stackrel{?}{\vdash} \{\langle x, y \rangle\}_{pk(k_B)}$$

CONSTRAINT SYSTEM

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$$y \stackrel{?}{=} pk(k_A)$$

CONSTRAINT SYSTEM

- One constraint system = one interleaving = several traces



$$pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)} \stackrel{?}{\vdash} \{\langle x, y \rangle\}_{pk(k_B)}$$

$$pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}, \{\langle x, N_b, pk(k_B) \rangle\}_y$$

$$y \stackrel{?}{=} pk(k_A)$$

CONSTRAINT SYSTEM

- One constraint system = one interleaving = several traces



Alice

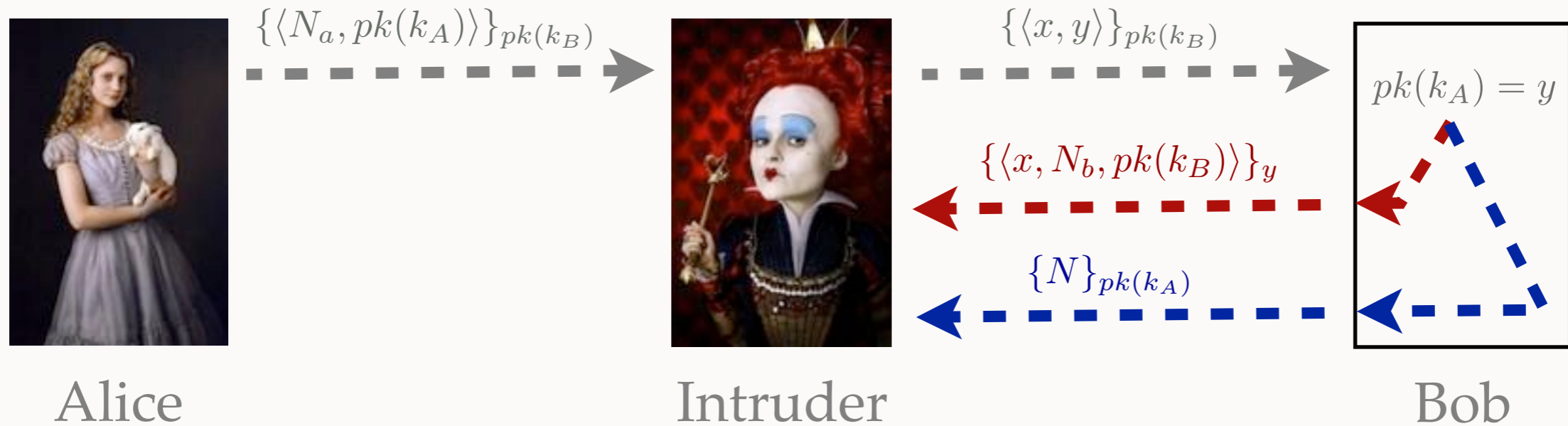
Intruder

Bob

$$\begin{aligned}
 D &: pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)} \stackrel{?}{\vdash} \{\langle x, y \rangle\}_{pk(k_B)} \\
 \Phi &: pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}, \{\langle x, N_b, pk(k_B) \rangle\}_y \\
 E &: y \stackrel{?}{=} pk(k_A)
 \end{aligned}$$

CONSTRAINT SYSTEM

- One constraint system = one interleaving = several traces



$$D : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)} \stackrel{?}{\vdash} \{\langle x, y \rangle\}_{pk(k_B)}$$

$$\Phi : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}, \{\langle x, N_b, pk(k_B) \rangle\}_y$$

$$E : y \stackrel{?}{=} pk(k_A)$$

$$D : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)} \stackrel{?}{\vdash} \{\langle x, y \rangle\}_{pk(k_B)}$$

$$\Phi : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}, \{N\}_{pk(k_A)}$$

$$E : y \neq pk(k_A)$$

CONSTRAINT SYSTEM

- One solution of a constraint system = one trace

$$D : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)} \vdash \{\langle x, y \rangle\}_{pk(k_B)}$$

$$\Phi : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}, \{\langle x, N_b, pk(k_B) \rangle\}_y$$

$$E : y = pk(k_A)$$

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$\Phi : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}, \{\langle x, N_b, pk(k_B) \rangle\}_y$

$E : y = pk(k_A)$

A solution is a pair of substitution (σ, θ) where :

- σ describe the messages
- θ describe how the messages are deduced

CONSTRAINT SYSTEM

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A solution is a pair of substitution (σ, θ) where :

- σ describe the messages
- θ describe how the messages are deduced

$$\sigma = \{x \rightarrow N_I; y \rightarrow pk(k_A)\}$$

CONSTRAINT SYSTEM

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$$D : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)} \vdash \{\langle x, y \rangle\}_{pk(k_B)} \quad X_1$$

$$\Phi : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}, \{\langle x, N_b, pk(k_B) \rangle\}_y$$

$$\quad \alpha x_1 \quad \alpha x_2 \quad \alpha x_3 \quad \alpha x_4 \quad \alpha x_5 \quad \alpha x_6$$

$$E : y = pk(k_A)$$

A solution is a pair of substitution (σ, θ) where :

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$$\Phi : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)}, \{\langle x, N_b, pk(k_B) \rangle\}_y$$

$$ax_1 \quad ax_2 \quad ax_3 \quad ax_4 \quad ax_5 \quad ax_6$$

$$E : y = pk(k_A)$$

A solution is a pair of substitution (σ, θ) where :

- σ describe the messages
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$$\sigma = \{x \rightarrow N_I; y \rightarrow pk(k_A)\}$$

$$\theta = \{X_1 \rightarrow \{\langle ax_4, ax_1 \rangle\}_{ax_2}\}$$

CONSTRAINT SYSTEM

- One solution of a constraint system = one trace

$$D : pk(k_A), pk(k_B), pk(k_C), N_I, \{\langle N_a, pk(k_A) \rangle\}_{pk(k_B)} \vdash \{\langle x, y \rangle\}_{pk(k_B)} \quad X_1$$

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$$ax_1 \quad ax_2 \quad ax_3 \quad ax_4 \quad ax_5 \quad ax_6$$

$$E : y = pk(k_A)$$

A solution is a pair of substitution (σ, θ) where :

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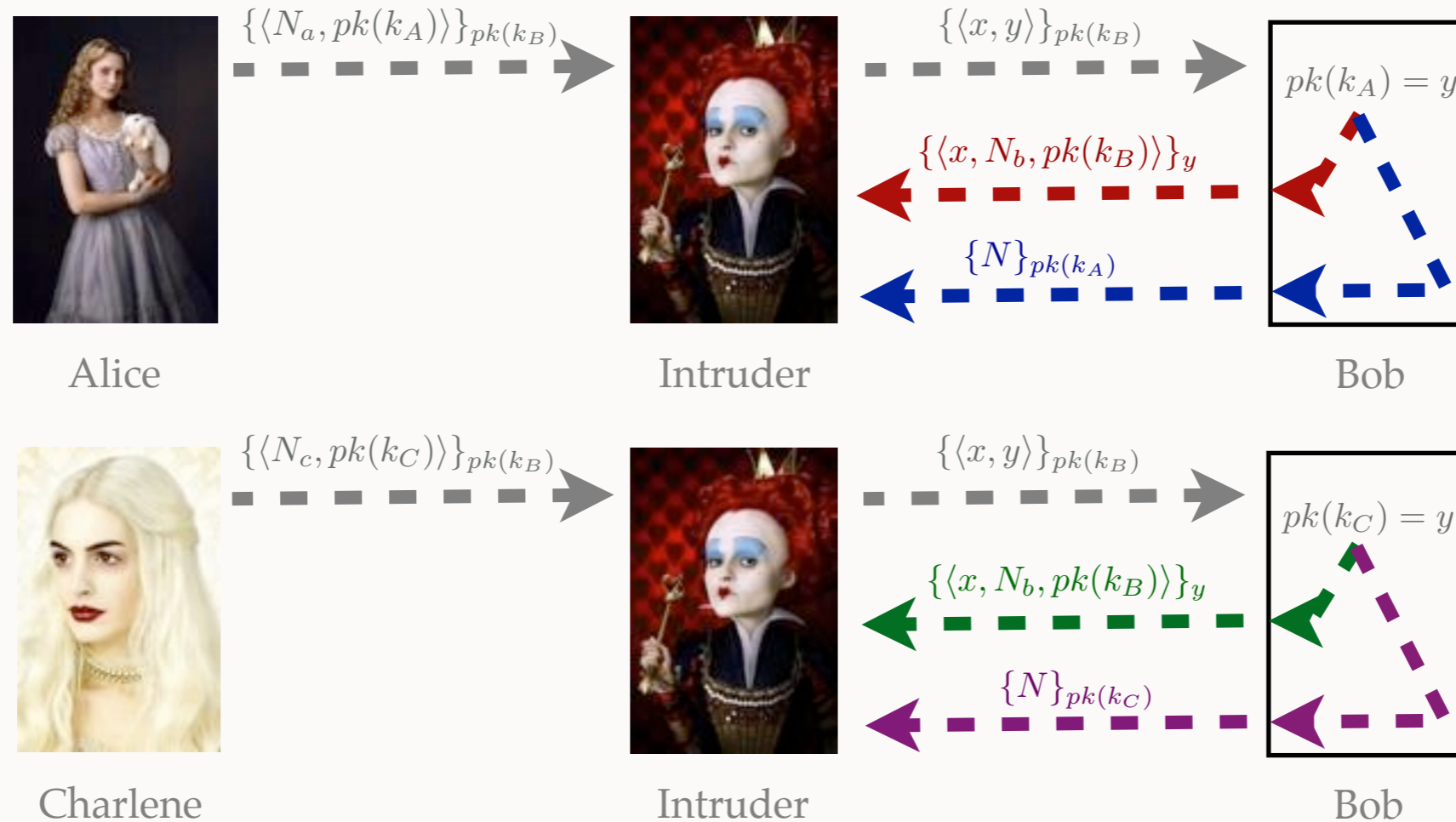
$$\sigma = \{x \rightarrow N_a; y \rightarrow pk(k_A)\}$$

$$\theta = \{X_1 \rightarrow \{\langle ax_4, ax_1 \rangle\}_{ax_2}\}$$

$$\theta = \{X_1 \rightarrow ax_5\}$$

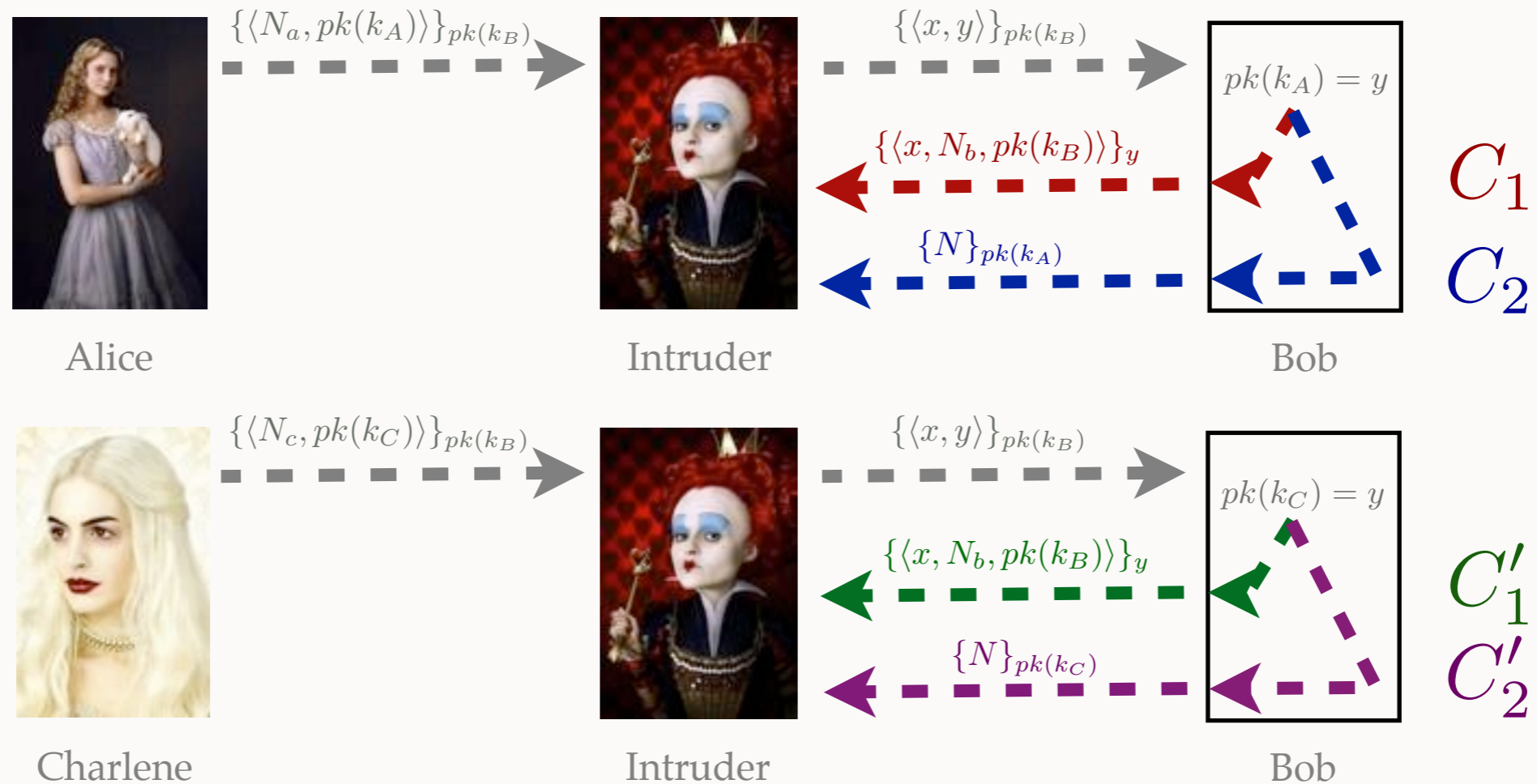
CONSTRAINT SYSTEM

- Set of constraint systems



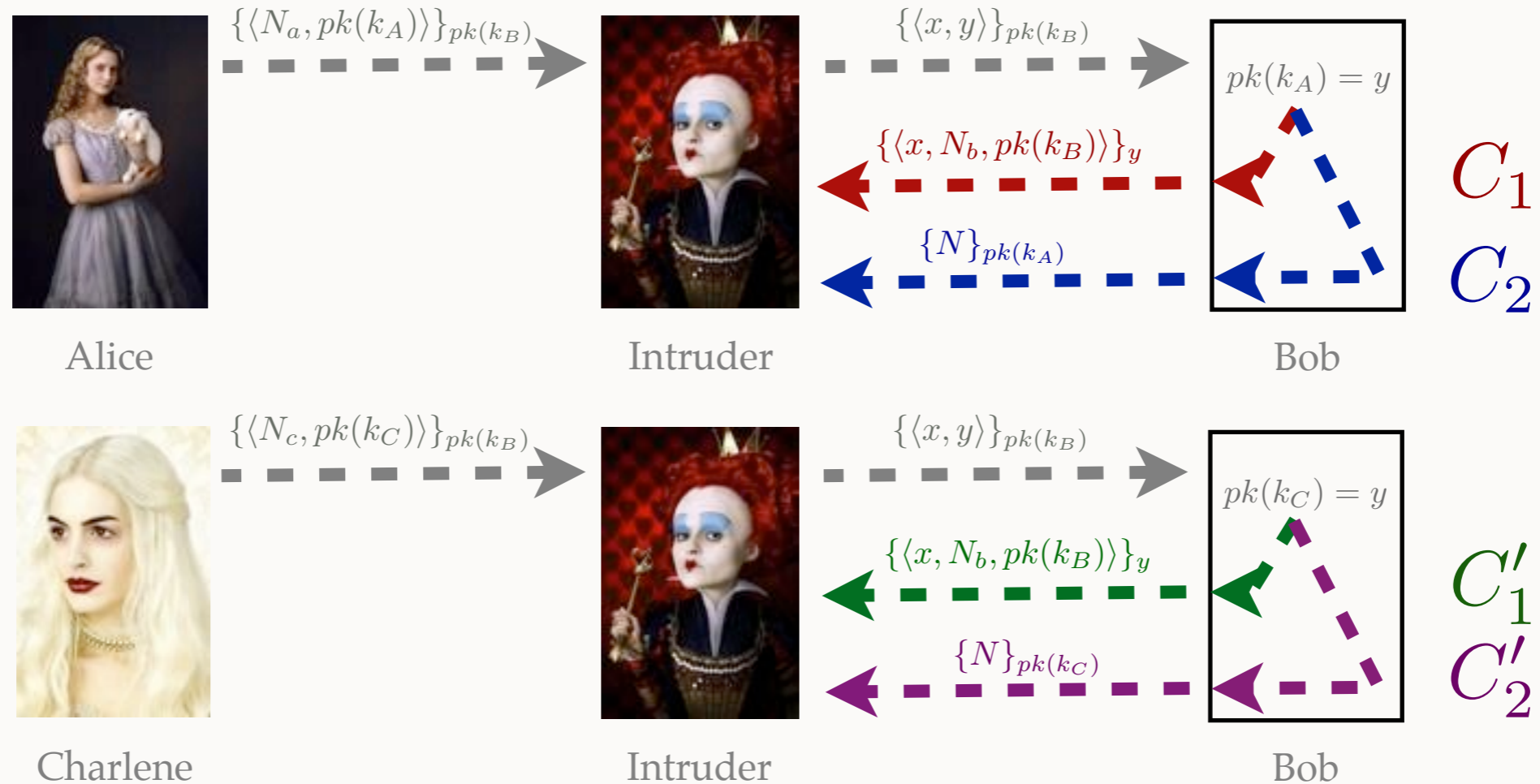
CONSTRAINT SYSTEM

- Set of constraint systems



CONSTRAINT SYSTEM

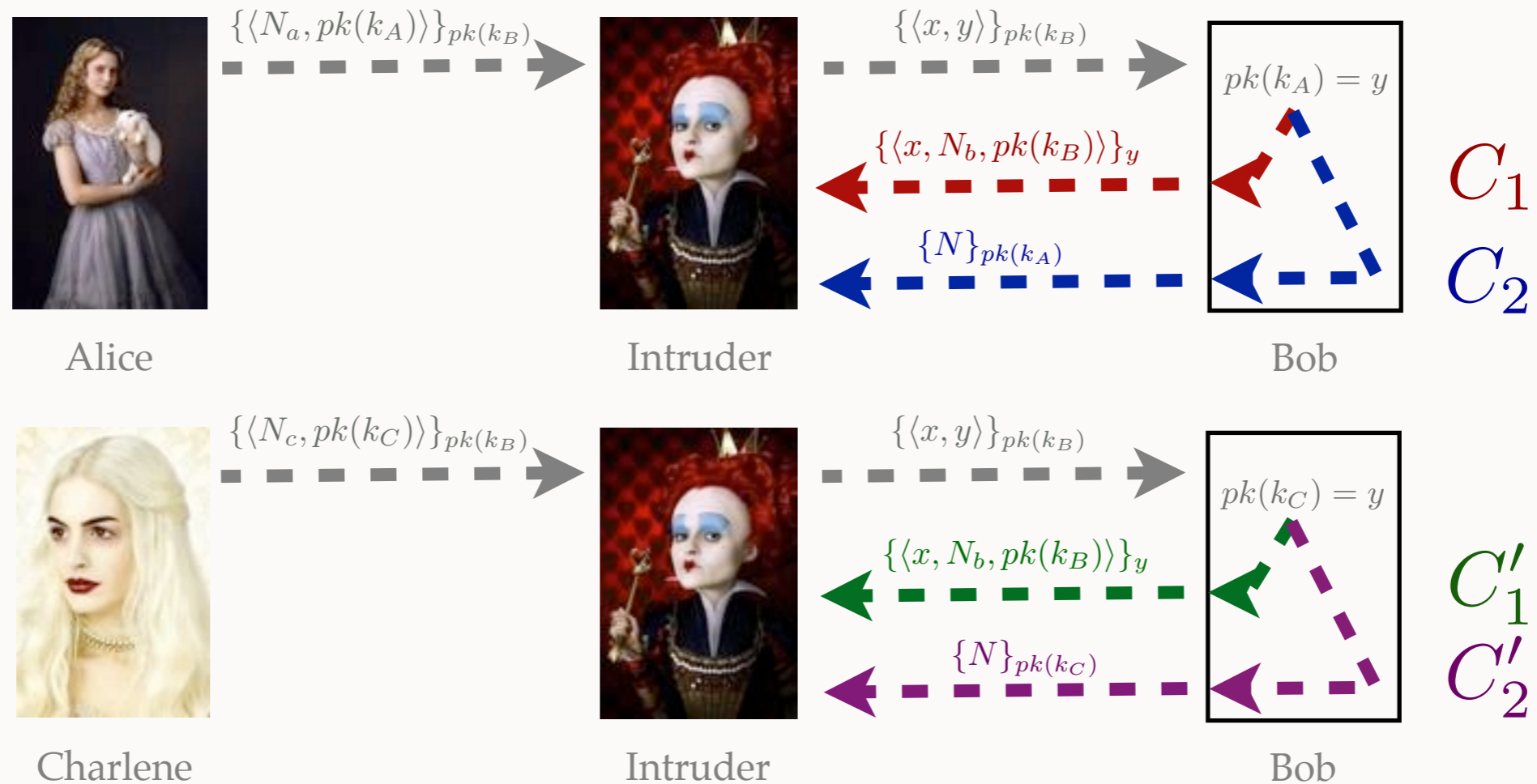
- Set of constraint systems



$$\{C_1; C_2\} \approx \{C'_1; C'_2\}$$

CONSTRAINT SYSTEM

- Set of constraint systems



Symbolic equivalence between sets of constraint systems

CONSTRAINT SYSTEM

- Symbolic equivalence between sets of constraint systems

To check whether P and P' are trace equivalent, we have to check that :

$$S \approx S', \text{ for all symbolic interleaving}$$

Symbolic equivalence $S \approx S'$

- For all $C \in S$, for all $(\theta, \sigma) \in \text{Sol}(C)$, there exists $C' \in S'$ and σ' such that $(\theta, \sigma') \in \text{Sol}(C')$ and $\Phi\sigma \sim \Phi'\sigma'$
- and conversely

CONSTRAINT SYSTEM

■ Previous works on constraint system

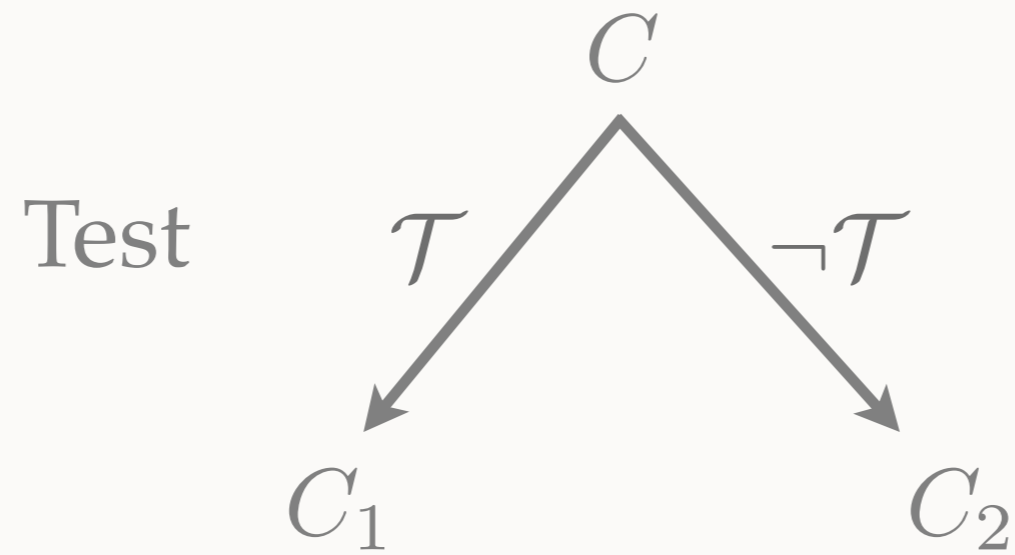
1. M. Baudet. *Sécurité des protocoles cryptographiques : aspects logiques et calculatoires*. Phd thesis
2. Y. Chevalier and M. Rusinowitch. *Decidability of equivalence of symbolic derivations*.
3. V. Cortier and S. Delaune. *A method for proving observational equivalence*.
4. A. Tiu and J. E. Dawson. *Automating open bisimulation checking for the spi calculus*.
5. V. Cheval, H. Comon-Lundh, S. Delaune. *Automating security analysis: symbolic equivalence of constraint systems*

Focus on :

- symbolic equivalence between two constraint systems (All)
- positive constraint system (no disequations) (All)
- subterm convergent equational theory (1,2 & 3)
- more restricted equational theory (4 & 5)

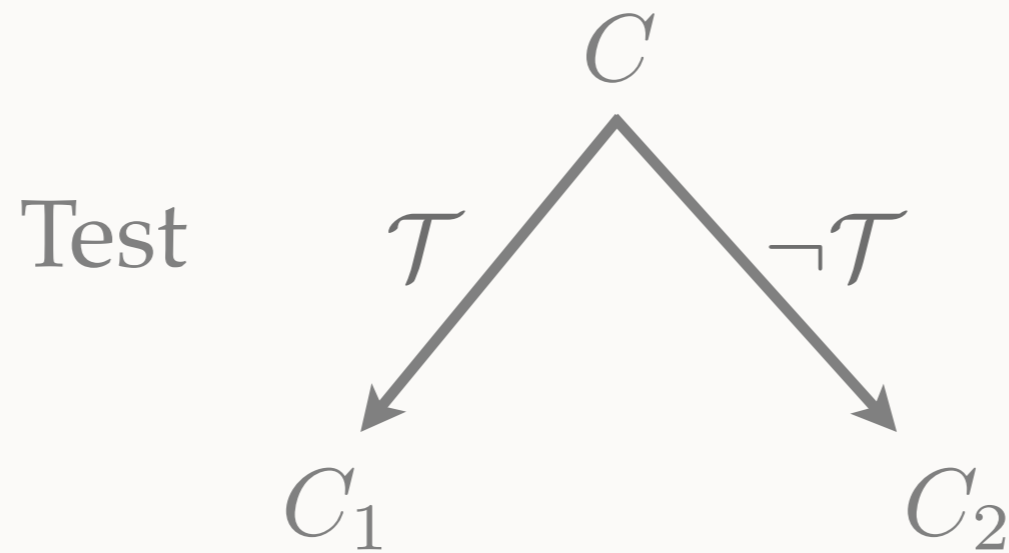
THE ALGORITHM

- Set of rules



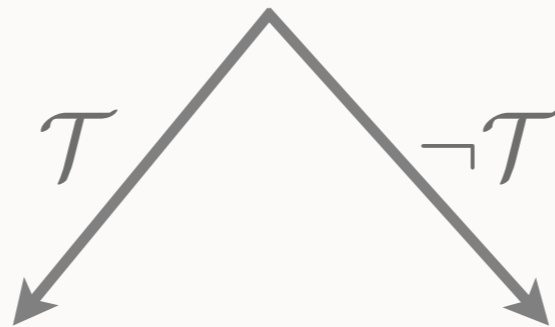
THE ALGORITHM

- Set of rules



- How to apply the rules :

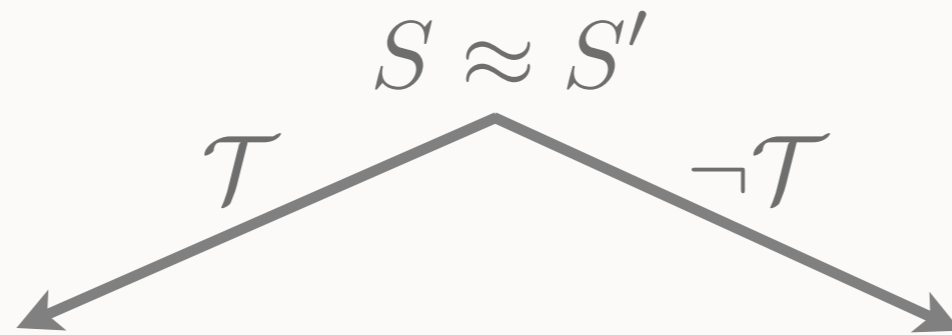
$$\{C^1; C^2; \dots\} \approx \{C^n; \dots\}$$



$$\{C_1^1; C_1^2; \dots\} \approx \{C_1^n; \dots\} \quad \{C_2^1; C_2^2; \dots\} \approx \{C_2^n; \dots\}$$

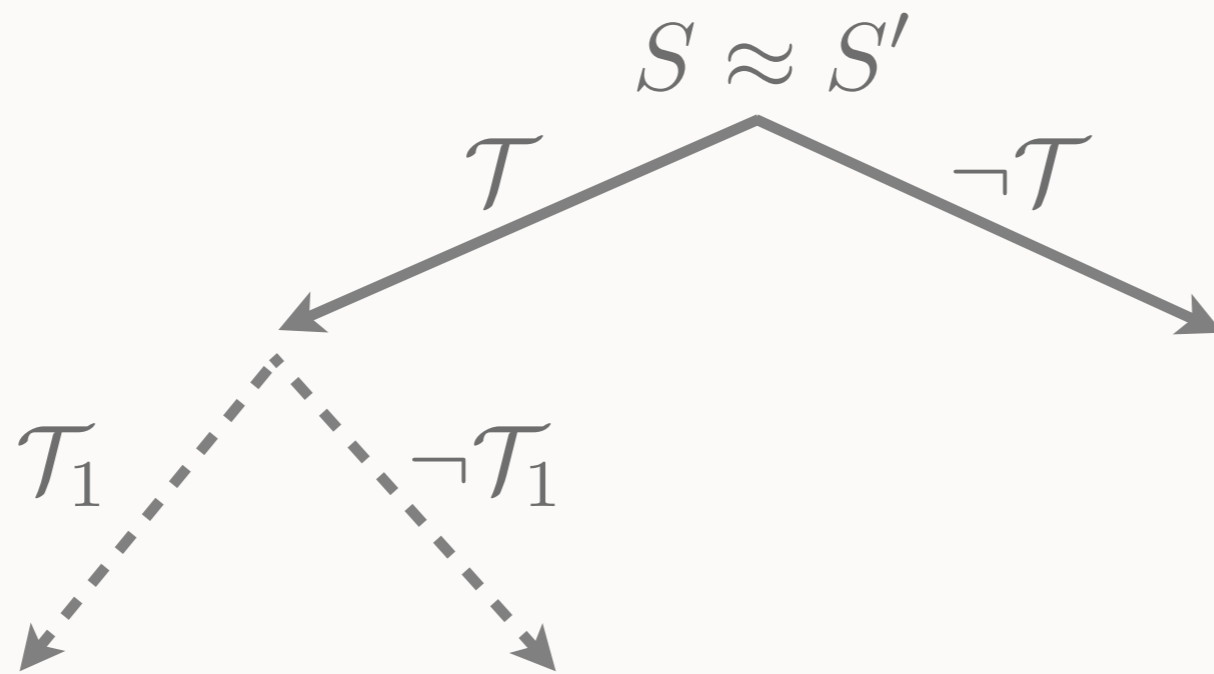
THE ALGORITHM

- A complete execution



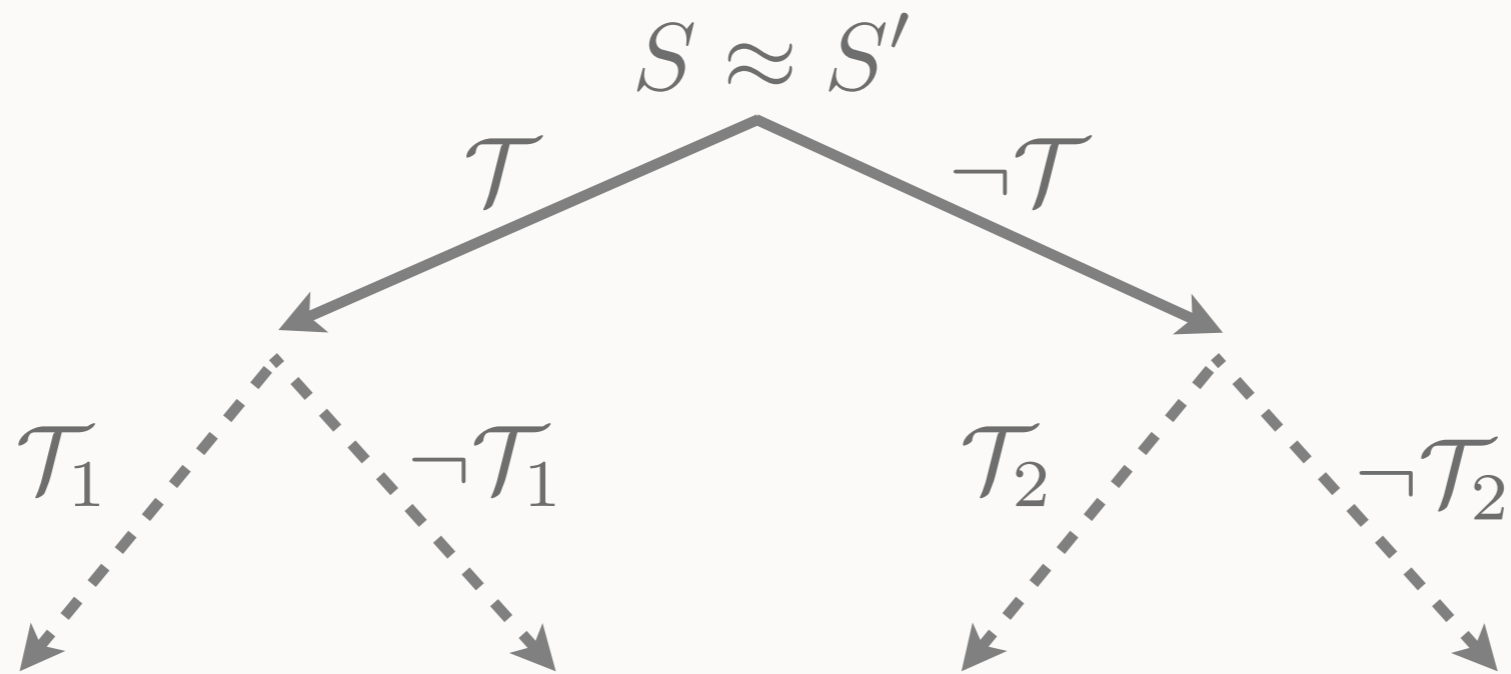
THE ALGORITHM

- A complete execution



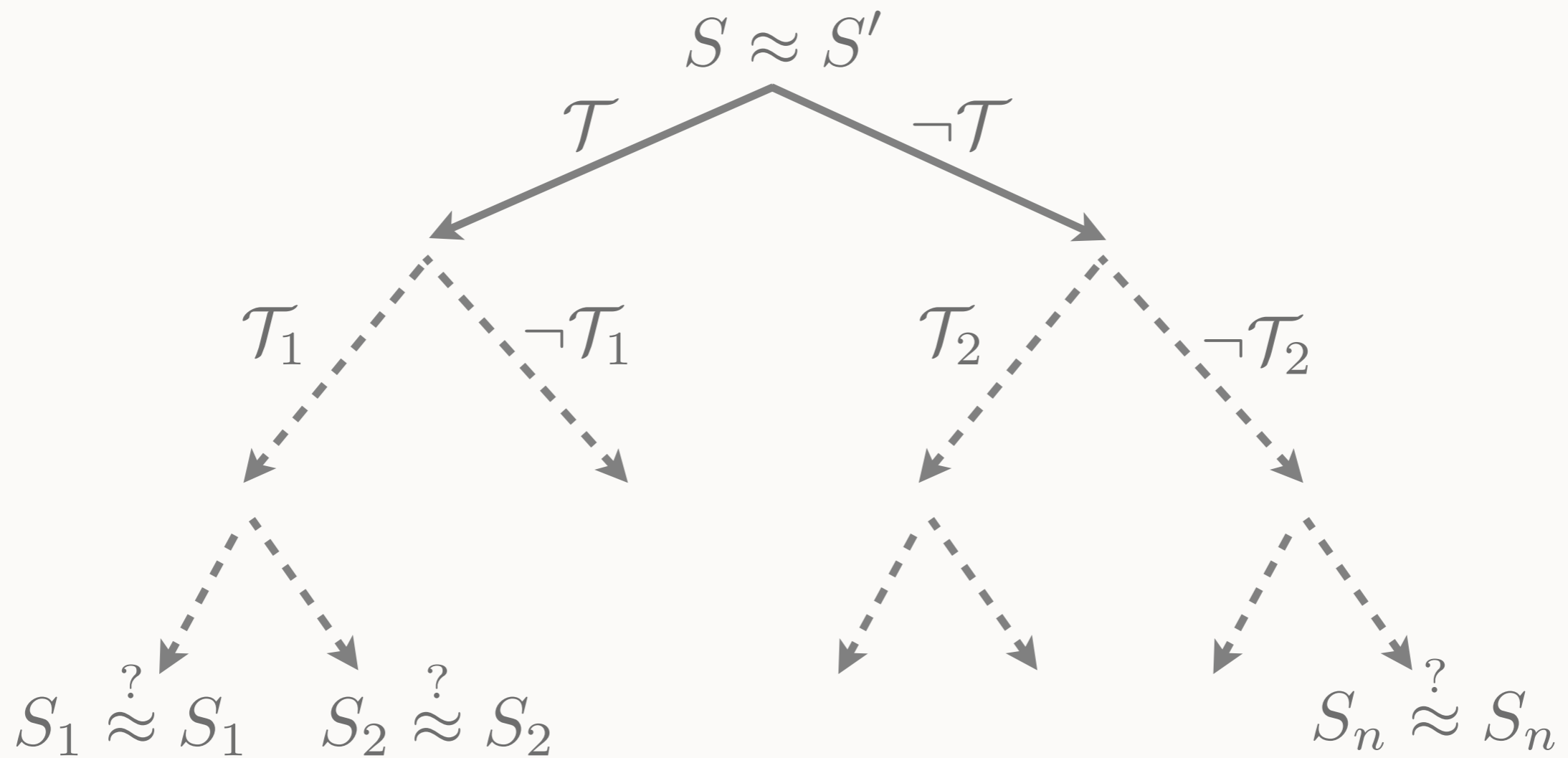
THE ALGORITHM

- A complete execution



THE ALGORITHM

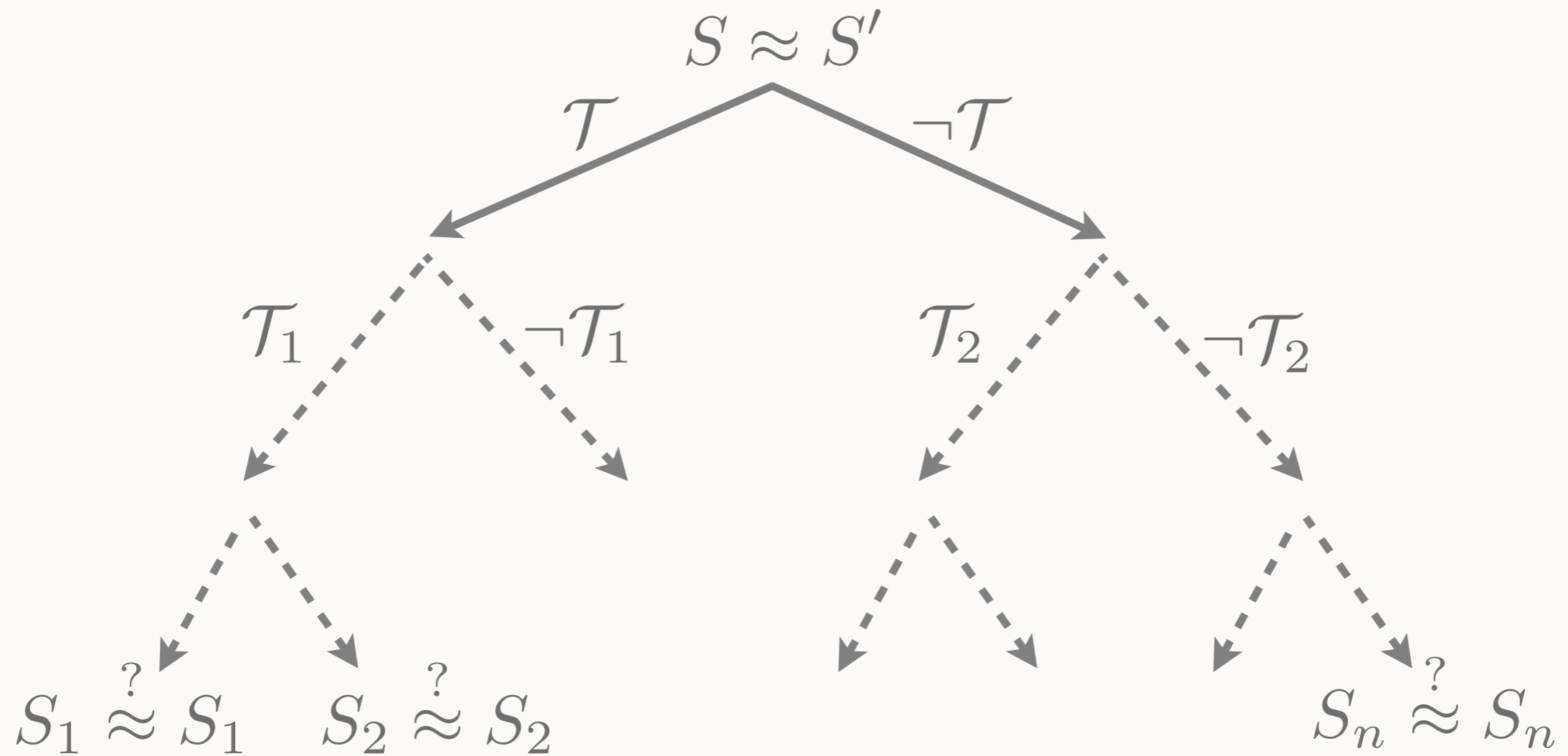
- A complete execution



The application of the rules creates a binary tree where each node is a pair of sets of constraint systems

THE ALGORITHM

- A complete execution



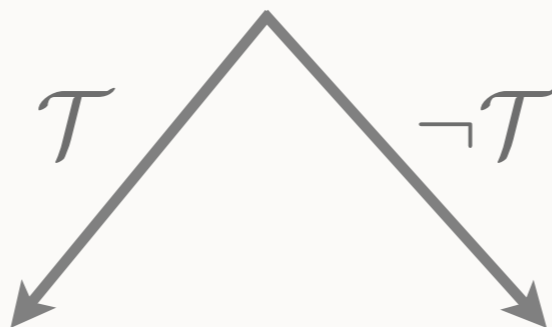
The symbolic equivalence is syntactically decided on each leaf

THE ALGORITHM

- Example of rule : Cons

Test $\mathcal{T} = \exists X_1, X_2$ s.t. $X = \text{enc}(X_1, X_2)$

$$\left\{ \begin{array}{l} \dots \\ T \vdash_X \text{enc}(u_1, u_2) \\ \dots \end{array} \right.$$



$$\left\{ \begin{array}{l} \dots \\ T \vdash_{X_1} u_1 \\ T \vdash_{X_2} u_2 \\ X = \text{enc}(X_1, X_2) \\ \dots \end{array} \right.$$

$$\left\{ \begin{array}{l} \dots \\ T \vdash_X \text{enc}(u_1, u_2) \\ \text{Top}(X) \neq \text{enc} \\ \dots \end{array} \right.$$

THE ALGORITHM

- The solved form of a constraint system

- Existence of solutions (Reachability)

$$\begin{array}{l} m_1, \dots, m_n \vdash x \\ m_1, \dots, m_n, \dots, m_{n'} \vdash y \end{array}$$

- Matching solutions (including disequations)

$$\begin{array}{l} a, b \vdash x \\ a, b, c \vdash y \\ x \neq y \end{array}$$

$$\begin{array}{l} a, b \vdash x \\ a, b, c \vdash y \\ x \neq f(y) \end{array}$$

- Static equivalence

$$\begin{array}{l} a, \{b\}_c \vdash x \\ a, \{b\}_c, c \vdash y \end{array}$$

$$\begin{array}{l} a, b \vdash x \\ a, b, c \vdash y \end{array}$$

RESULT

Let (S_0, S'_0) be an initial pair of set of constraint systems, we have :

(S, S')

(S, S')

RESULT

Let (S_0, S'_0) be an initial pair of set of constraint systems, we have :

If all leaves (S, S') on the tree satisfy the testing condition then $S_0 \approx S'_0$.

(S, S')

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RESULT

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If all leaves (S, S') on the tree satisfy the testing condition then $S_0 \approx S'_0$.

If $S_0 \approx S'_0$ then all leaves (S, S') on the tree satisfy the testing condition.

The strategy terminates

FUTURE WORK

■ Contribution

Decision procedure for trace equivalence

- Infinitely many traces are represented by symbolic constraint system
- + Protocol possibly non-determinate and with non trivial else branches
- + Private channels
- Finite set of cryptographic primitives : symmetric and asymmetric encryption, pairing and signature
- Bounded number of sessions (no replication in the process algebra)

■ Future work

- Efficient implementation (application on more case studies)
- More cryptographic primitives
- Link with ProVerif

TERMINATION

- The disequations problem

$$a, b \vdash x_1$$

$$D : a, b \vdash x_2$$

$$a, b \vdash y$$

$$E : [x_1 \neq y \vee x_2 \neq a] \wedge y \neq \langle x_1, x_2, b \rangle$$

TERMINATION

- The disequations problem

$$E : [x_1 \neq y \vee x_2 \neq a] \wedge y \neq \langle x_1, x_2, b \rangle$$

TERMINATION

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TERMINATION

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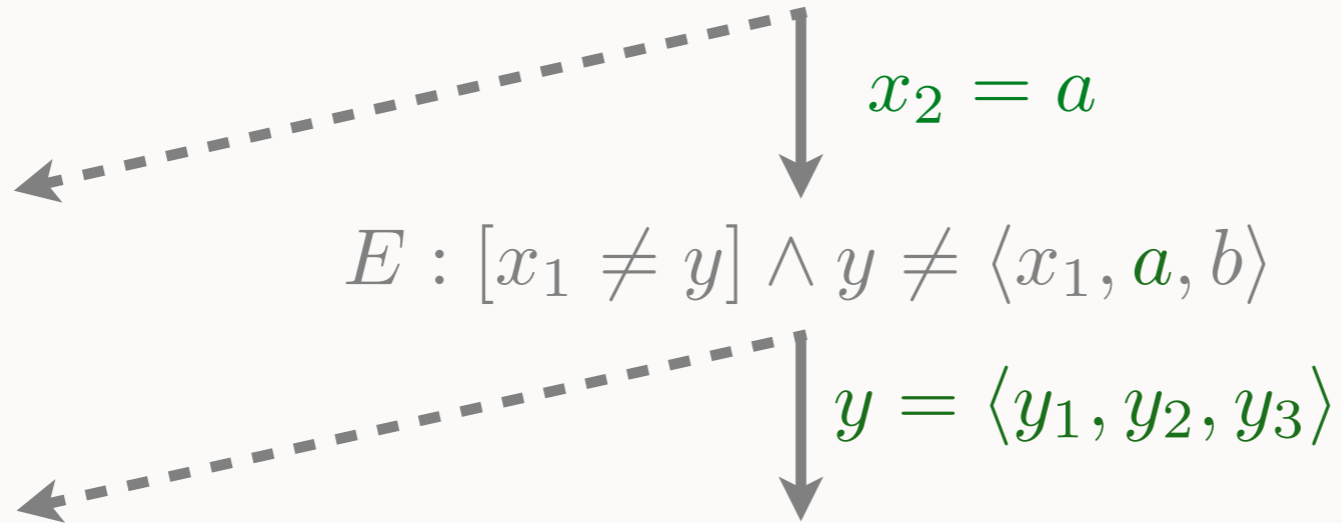


$$E : [x_1 \neq y] \wedge y \neq \langle x_1, a, b \rangle$$

TERMINATION

- The disequations problem

$$E : [x_1 \neq y \vee x_2 \neq a] \wedge y \neq \langle x_1, x_2, b \rangle$$



TERMINATION

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$$E : [x_1 \neq y \vee x_2 \neq a] \wedge y \neq \langle x_1, x_2, b \rangle$$



$$E : [x_1 \neq y] \wedge y \neq \langle x_1, a, b \rangle$$



$$E : [x_1 \neq \langle y_1, y_2, y_3 \rangle] \wedge \langle y_1, y_2, y_3 \rangle \neq \langle x_1, a, b \rangle$$

TERMINATION

- The disequations problem

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TERMINATION

- The disequations problem

$$E : [x_1 \neq y \vee x_2 \neq a] \wedge y \neq \langle x_1, x_2, b \rangle$$

$x_2 = a$

$$E : [x_1 \neq y] \wedge y \neq \langle x_1, a, b \rangle$$

$y = \langle y_1, y_2, y_3 \rangle$

$$E : [x_1 \neq \langle y_1, y_2, y_3 \rangle] \wedge \langle y_1, y_2, y_3 \rangle \neq \langle x_1, a, b \rangle$$

$E : [x_1 \neq \langle y_1, y_2, y_3 \rangle] \wedge [y_1 \neq x_1 \vee y_2 \neq a \vee y_3 \neq b]$

TERMINATION

- The disequations problem

$$E : [x_1 \neq y \vee x_2 \neq a] \wedge y \neq \langle x_1, x_2, b \rangle$$

$$x_2 = a$$

$$E : [x_1 \neq y] \wedge y \neq \langle x_1, a, b \rangle$$

$$y = \langle y_1, y_2, y_3 \rangle$$

$$E : [x_1 \neq \langle y_1, y_2, y_3 \rangle] \wedge \langle y_1, y_2, y_3 \rangle \neq \langle x_1, a, b \rangle$$

$$E : [x_1 \neq \langle y_1, y_2, y_3 \rangle] \wedge [y_1 \neq x_1 \vee y_2 \neq a \vee y_3 \neq b]$$

$$y_3 = b$$

TERMINATION

- The disequations problem

$$E : [x_1 \neq y \vee x_2 \neq a] \wedge y \neq \langle x_1, x_2, b \rangle$$

$x_2 = a$

$$E : [x_1 \neq y] \wedge y \neq \langle x_1, a, b \rangle$$

$y = \langle y_1, y_2, y_3 \rangle$

$$E : [x_1 \neq \langle y_1, y_2, y_3 \rangle] \wedge \langle y_1, y_2, y_3 \rangle \neq \langle x_1, a, b \rangle$$

$y_3 = b$

$$E : [x_1 \neq \langle y_1, y_2, y_3 \rangle] \wedge [y_1 \neq x_1 \vee y_2 \neq a \vee y_3 \neq b]$$

$y_3 = b$

$$E : [x_1 \neq \langle y_1, y_2, b \rangle] \wedge [y_1 \neq x_1 \vee y_2 \neq a]$$